## Spring Block 1 Place value (within 20)

| Step 1 | Count within 20 |
| :---: | :---: |
| Step 2 | Understand 10 |
| Step 3 | Understand 11, 12 and 13 |
| Step 4 | Understand 14, 15 and 16 |
| Step 5 | Understand 17, 18 and 19 |
| Step 6 | Understand 20 |
| Step 7 | 1 more and 1 less |
| Step 8 | The number line to 20 |

## Small steps

Step 9
Use a number line to 20

| Step 10 | Estimate on a number line to 20 |
| :--- | :--- |
| Step 11 | Compare numbers to 20 |
| Step 12 | Order numbers to 20 |

## Count within 20

## Notes and guidance

In the Autumn term, children learnt the numbers to 10. In this small step, they extend that learning to count to 20

Provide regular opportunities for children to verbally count to 20, for example counting how many children are present or how many beanbags there are in a bucket. Children can find counting through the teen numbers difficult, as the number names do not have the same regular 1 to 9 pattern that they hear once they count beyond 20 . Use concrete resources to support children to see the "10-and-a-bit" structure of teen numbers.

Number tracks can support children in counting on and back to 20. "I count, you count" activities allow children to practise continuing the count from different starting points.

## Things to look out for

- Children may find the numbers $11,12,13$ and 15 confusing, as they cannot hear the $1,2,3$ and 5 within them.
- Children may find writing teen numbers tricky, in particular reversing the digits. For example, when saying 16, they hear the 6 first, so may write 61


## Key questions

- What number comes after $\qquad$ ?
- What number comes before $\qquad$ ?
- Which numbers sound different? Why?
- Which numbers after 10 do not include "teen"?
- How can you count 20 cubes/counters/pencils/glue sticks?
- What songs do you know that count to 20 ?


## Possible sentence stems

- The number that comes after $\qquad$ is $\qquad$
- The number that comes before $\qquad$ is $\qquad$
- There are $\qquad$ cubes.


## National Curriculum links

- Count to and across 100 , forwards and backwards, beginning with zero or 1 , or from any given number
- Identify and represent numbers using objects and pictorial representations including the number line, and use the language of: equal to, more than, less than (fewer), most, least


## Count within 20

## Key learning

Read 1 to 20 Animals Aplenty by Katie Viggers.
Show the pages from the book with the text hidden and ask children to count the animals on each page. Challenge them to work out the hidden rhyme.

For this game, you need a 1-3 dice and a pebble.
Draw a large number track from 0 to 20 on the playground and place a pebble on number 10

Player 1 aims to get to 20
They roll the dice and move the pebble that number of places towards 20 , counting out loud, for example 11, 12, 13
Player 2 aims to get to zero.
They roll the dice and move the pebble that number of places towards zero, counting out loud, for example 12, 11, 10
The winner is the first player to reach their target number.

Put children into three groups.
Point to a group and ask them to begin counting from 1. When you point to another group, they should continue the count. Keep switching between groups.
To add challenge, point up when you want the children to count on from the last number counted and point down for them to count back.

- Match the pictures to the numbers on the number track.


| 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

## Count within 20

## Reasoning and problem solving

Here are some number cards.


Which of the numbers will Jo say?


Which of the numbers will Ron say?

Mr Lee keeps hens and sheep.


He counts 14 legs altogether.
How many hens and sheep could Mr Lee have?

Compare answers with a partner.

2 hens and 3 sheep
3 hens and 2 sheep
5 hens and 1 sheep

## Understand 10

## Key questions

- How many ways can you make 10 ?
- How do you know that you have made 10?
- Is 10 greater than 9 or less than 9 ?
- How many ones make 10 ?
- If you have one full ten frame, what number have you got?
- What is this piece of base 10 worth? How do you know?


## Possible sentence stems

- The ten frame is full, so I know that I have made $\qquad$
- There are $\qquad$ ones in 10
- There are $\qquad$ ones in $\qquad$ ten.


## National Curriculum links

- Identify and represent numbers using objects and pictorial representations including the number line, and use the language of: equal to, more than, less than (fewer), most, least
- Count, read and write numbers to 100 in numerals; count in multiples of $2 s, 5 s$ and $10 s$


## Understand 10

## Key learning

Give one child 10 single cubes and another child a tower of 10 cubes. Ask which is more. Use the cubes to demonstrate that 10 ones and 1 ten are equivalent.

Repeat with 10 loose counters and 10 counters on a ten frame.

Show children 10 counters arranged in different ways. How do they see the 10 each time?


Ask children to count out 10 counters and arrange them in different ways.

What else do they notice about the composition of 10 ?

- Which pictures show 10 ?


Provide a variety of sets of different-sized objects, ensuring that some sets have 10 items and some do not. Ask children to fill ten frames to help them to sort the sets into " 10 " and "not 10 ".

Challenge them to explain how to change the sets that are not 10 into 10

Give each child a tower of cubes from 1 to 9 . Ask them to get into pairs so that each pair of children can combine their cubes to make 10

A similar activity can be done using number pieces.

## Understand 10

## Reasoning and problem solving

Tiny has made 10 using three different-coloured counters on a ten frame.


Make 10 using three different-coloured counters on a ten frame.

How many ways can you find?

multiple possible answers, e.g.

8, 1, 1
7, 2, 1

Kim has two red buckets and one yellow bucket.


She has 10 shells.
Kim puts her shells into the buckets.
The red buckets have the same number of shells inside.

How many shells could there be in each of Kim's buckets?

What do you notice about the number of shells in the yellow bucket?

$$
\begin{aligned}
& 0+0+10 \\
& 1+1+8 \\
& 2+2+6 \\
& 3+3+4 \\
& 4+4+2 \\
& 5+5+0
\end{aligned}
$$

## Understand 11, 12 and 13

## Key questions

- How can you show me 11 in three different ways?
- How much more than 10 is 12 ?
- How can you write the numbers 11,12 and 13 ?
- Can you see 11/12/13 anywhere in the classroom?
- Does anyone have a brother or sister who is 11,12 or 13 ?
- How many ones are there in 13 ?
- What is the same and what is different about 11,12 and 13 ?


## Possible sentence stems

- 11 has ___ ten and ___ one.
- 12 has $\qquad$ ten and $\qquad$ ones.
- 13 has $\qquad$ ten and $\qquad$ ones.


## National Curriculum links

- Count to and across 100, forwards and backwards, beginning with zero or 1 , or from any given number
- Read and write numbers from 1 to 20 in numerals and words


## Understand 11, 12 and 13

- Match the pictures to the numbers.

Show children 10 counters on a ten frame.
Ask how many there will be if you add one more counter. Discuss whether you can fit 11 counters on a ten frame. Build 11, emphasising 1 full ten and 1 more, linking this to how we write the numeral 11

Repeat for 12 and 13
11

12

13


- Which pictures show 13 ?

Quickly show a picture of 11,12 or 13 , making sure that the " 10 -and-a-bit" structure is clear. Then hide the picture.
Ask children which number they saw. Can they explain how they know?


12
13



- Match the numerals to the number words.


## Understand 11, 12 and 13

## Reasoning and problem solving



Discuss answers as a class.

## Understand 14, 15 and 16

## Key questions

- How can you show me 14/15/16 in three different ways?
- How much more than 10 is $14 / 15 / 16$ ?
- How can you write the numbers 14,15 and 16 ?
- Can you see 14/15/16 anywhere in the classroom?
- Does anyone have a brother or sister who is 14,15 or 16 ?
- How many ones are there in 16 ?
- What is the same and what is different about 14,15 and 16 ?


## Possible sentence stems

- 14 has___ ten and ___ ones.
- 15 has $\qquad$ ten and $\qquad$ ones.
- 16 has $\qquad$ ten and $\qquad$ ones.


## National Curriculum links

- Count to and across 100, forwards and backwards, beginning with zero or 1 , or from any given number
- Read and write numbers from 1 to 20 in numerals and words


## Understand 14, 15 and 16

- Write the number shown on the ten frames in numerals and words.


Use ten frames to show fifteen and fourteen.

- Complete the table.

| Numerals | Word | Picture |
| :---: | :---: | :---: |
| 14 |  |  |
|  |  | 000000000000000 |
|  | sixteen |  |

- Complete the part-whole models.




## Understand 14, 15 and 16

## Reasoning and problem solving

Ron uses counters to make two numbers.


What is the same? What is different?
Which group of counters is easier to count?
Why?


Tiny makes a part-whole model.


What mistake has Tiny made?

Tiny has 1 full ten and 5 more cubes.
The number is 15

## Understand 17, 18 and 19

## Key questions

- How can you show me 17/18/19 in three different ways?
- How much more than 10 is $17 / 18 / 19$ ?
- How can you write the numbers 17,18 and 19 ?
- Can you see 17/18/19 anywhere in the classroom?
- How many ones are there in 19 ?
- What is the same and what is different about 17,18 and $19 ?$
- When you make 18 on a ten frame, how many spaces are empty?


## Possible sentence stems

- 17 has $\qquad$ ten and $\qquad$ ones.
- 18 has $\qquad$ ten and $\qquad$ ones.
- 19 has $\qquad$ ten and $\qquad$ ones.
- There are $\qquad$ empty spaces on the ten frame.


## National Curriculum links

- Count to and across 100, forwards and backwards, beginning with zero or 1 , or from any given number
- Read and write numbers from 1 to 20 in numerals and words


## Key learning

Show children 17 on ten frames.
What do they notice about 17 ?
Ask children to use counters and ten frames to make 18 and 19 and to talk to a partner about what they notice.

Play Snap using a set of cards with each card showing a numeral, word or representation for 17,18 or 19

When children shout
"Snap!", ask them to explain why the numbers are the same.


Ask children to write three numbers between 10 and 20 Show them a number (varying the representations). If they have written that number, they cross it out. The first child to cross out all three of their numbers wins the game.

- Match the pictures to the numbers.


seventeen
- Use the ten frames to complete the sentence.


17 has $\qquad$ ten and $\qquad$ ones.

Use ten frames to show 18 and 19

- Complete the number tracks.

| 10 | 11 | 12 | 13 |  | 15 | 16 |  |  | 19 | 20 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |


| 20 |  | 18 |  | 16 | 15 | 14 |  | 12 | 11 | 10 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

## Reasoning and problem solving



## Understand 20

## Key questions

- How many ways can you make 20?
- How do you know that you have made 20?
- Is 20 greater than 19 or less than 19 ?
- How many ones make 20?
- How many tens make 20?
- If you have two full ten frames, what number have you got?
- How many pieces of base 10 do you need to make 20?


## Possible sentence stems

- Two ten frames are full, so I know that I have made $\qquad$
- There are $\qquad$ ones in 20
- There are $\qquad$ tens in 20


## National Curriculum links

- Identify and represent numbers using objects and pictorial representations including the number line, and use the language of: equal to, more than, less than (fewer), most, least
- Count, read and write numbers to 100 in numerals; count in multiples of $2 \mathrm{~s}, 5 \mathrm{~s}$ and 10 s


## Understand 20

## Key learning

Hide small objects outside and provide two ten frames for each group of children.
The groups race to find 20 objects and fill their ten frames. Prompt children to tell you how many objects they have found and how many more they need to make 20

Show representations of numbers and ask children to decide if the number shown is 20 or not 20 , explaining how they know.

Read One is a Snail, Ten is a Crab by April Pulley Sayre and Jeff Sayre.

Remind children that 20 is 2 crabs.
Ask children to find different ways of making 20 using the animals in the book.

- Which pictures show 20?


Children can play this game in pairs or small groups. They need a number track from 0 to 20, a 1-3 dice and some counters.

They start from zero and take turns to roll the dice and count on the corresponding number of jumps. For example, if Tom is on 6 and rolls a 3 , he counts $7,8,9$ as he moves his counter along the track.

The first child to reach exactly 20 wins.

## Understand 20

## Reasoning and problem solving



Ann is throwing beanbags into two hoops.

She scores 10 for a beanbag in the small hoop.

She scores 5 for a beanbag in the large hoop.


How can Ann score 20?
How many ways can you find?


10 and 10
5,5,5 and 5
10, 5 and 5

## Key questions

- How can you show the number $\qquad$ ?
- How can you find 1 more?

How does this change the number?
Which digit changes?

- How can you find 1 less?

How does this change the number?

- What is the same and what is different about finding 1 more and finding 1 less?
- When you are finding 1 more or 1 less, which digit changes? Is it always the same digit?


## Possible sentence stems

- $\qquad$ is 1 more than $\qquad$
- $\qquad$ is 1 less than $\qquad$
- 1 more than $\qquad$ is $\qquad$
- 1 less than $\qquad$ is $\qquad$


## National Curriculum links

- Given a number, identify 1 more and 1 less


## 1 more and 1 less

## Key learning

Reread 1 to 20 Animals Aplenty by Katie Viggers.
Draw children's attention to the 1 more pattern in the book. Build towers of cubes to represent the animals on each page and to show the 1 more step pattern.

Look at the 11 to 20 counting pattern on the last page of 1 to 20 Animals Aplenty.
Ask children to build or draw their own 11 to 20 step patterns. This could be done using resources outside or chalked onto the playground.

- Make 1 more and 1 less than each number.

- Use cubes to make 1 more and 1 less than the numbers.

- Write numbers to fill in the boxes.

Use base 10 to help you.


- Use the number track to help you complete the sentences.

| 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

- $\qquad$ is 1 more than 13 - $\qquad$ is 1 less than 19
- 13 is 1 more than $\qquad$ - 19 is 1 less than $\qquad$


## 1 more and 1 less

## Reasoning and problem solving

Dan is 1 year older than his sister.
Dan's sister is 1 year older than Dan's brother.

Dan's brother is 13
How old is Dan's sister?
How old is Dan?

Use the numbers from 11 to 20 to fill in the boxes.



14 years old

15 years old
multiple possible answers, e.g.
18, 17
12, 11

Max thinks of a number.


What is Max's number?
How do you know?
Kim thinks of a number.


What is Kim's number?
How do you know?

## Key questions

- How can you label the number line? How do you know where to put the numbers?
- What does each mark on the number line represent?
- Where does the number line start/end?
- How can you use a number line to decide which number is greater?
- How much is each jump on the number line?


## Possible sentence stems

- The first number on the number line is $\qquad$
- The last number on the number line is $\qquad$


## National Curriculum links

- Count to and across 100, forwards and backwards, beginning with zero or 1 , or from any given number
- Identify and represent numbers using objects and pictorial representations including the number line, and use the language of: equal to, more than, less than (fewer), most, least


## The number line to 20

- Complete the number lines.


What is the same about the number lines? What is different?

- Complete the number lines.

- Use a number line from 0 to 20
- Circle the number 13
- Circle the number 20


## The number line to 20

## Reasoning and problem solving

Tiny has put number cards on two number lines.
Spot the mistake in each number line.


Draw a number line with a mistake for a partner to spot.

16 is missing.

15 and 17 are the wrong way round.

Sam is thinking of a number.


What could Sam's number be?
Compare answers with a partner.
any number greater than 13 and less than or equal to 20

## Key questions

- How can you label the number line? How do you know where to put the numbers?
- What does each mark on the number line represent?
- Where does the number line start/end?
- How do you find 1 more/less on a number line?
- What does each jump on the number line represent?


## Possible sentence stems

- The first number on the number line is $\qquad$
- The last number on the number line is $\qquad$
- To find 1 more/less, I need to ...


## National Curriculum links

- Count to and across 100, forwards and backwards, beginning with zero or 1 , or from any given number
- Identify and represent numbers using objects and pictorial representations including the number line, and use the language of: equal to, more than, less than (fewer), most, least


## Use a number line to 20

## Key learning

Use chalk to draw a large 0-20 number line on the playground.
Ask a child to start at 9 and jump to 17, one division at a time. Which numbers do they land on?

Can children find 1 more and 1 less than 15?
Can they find all the numbers that are greater
than 11 ? Less than 14 ?
Can they find all the numbers in between 12 and 18 ?

- Ann counts from 8 to 15

Circle all the numbers that she will say.


- Circle all the numbers that are greater than 7

- Circle all the numbers that are less than 13

- What numbers are the arrows pointing to?

- Label 15,12 and 9 on the number line.


Label 7, 17 and 19 on the number line.


## Use a number line to 20

## Reasoning and problem solving

Ask children to pick a number on the number line.


Can they tell you how many jumps there are from zero to their number? How many jumps are there from their number to 20? Is their number closer to zero or closer to 20?

Repeat with different numbers.
Ask children what they notice about the two sets of jumps each time.
multiple possible answers, e.g. 15
15 jumps from zero to 15
5 jumps from 15 to 20

The two sets of jumps always total 20


Do you agree with Tiny?
Why?

Which numbers are hidden by the card?

$13,14,15$

## Notes and guidance

In this small step, children are asked to estimate for the first time. This is a new word for children to learn. Previously, they may have been asked to "guess" and make predictions.

When children are beginning to estimate on a number line, take time to explore the halfway point. Where do they think halfway is? How do they know? What informal measurements could they use to check? (For example, steps in the playground.)
Some children may initially struggle to estimate. Conversations with other children are vital to develop understanding. Some children may find not having an exact answer difficult and need time to grasp the idea of estimating.
Children need to be confident using a number line before being able to estimate. For example, if they are estimating where 4 is on a blank number line from zero to 10 , they need to be able to reason that it will be less than halfway.

## Things to look out for

- Some children may be reluctant to estimate in case they get it wrong. Introduce estimation in a fun, game-like way so that children feel comfortable having a go and discussing their reasons.


## Key questions

- What does "estimate" mean?
- Can you find halfway?
- What number is halfway on the number line? Is 7 more or less than the number?
- Will halfway on the number line always be 5 ? What if the number line starts at zero and ends at 20? What number is halfway now?
- Can you explain your thinking?
- Where is 15 on the number line? How do you know?


## Possible sentence stems

- $\qquad$ is halfway along the number line.
- $\qquad$ is closer to $\qquad$ than $\qquad$


## National Curriculum links

- Count to and across 100, forwards and backwards, beginning with zero or 1 , or from any given number
- Identify and represent numbers using objects and pictorial representations including the number line, and use the language of: equal to, more than, less than (fewer), most, least


## Estimate on a number line to 20

- Estimate where 4 belongs on the number line.


Estimate where 14 belongs on the number line.


What is the same? What is different?

- Estimate where 15 belongs on each number line.


What is the same? What is different?

- Draw and label number lines from 0 to 10 and 0 to 20

Which numbers will you mark on your lines first?

## Reasoning and problem solving



Tiny is trying to draw a number line from 0 to 20


What is wrong with Tiny's number line? How would you draw the number line?

Tiny will not have enough room for all the numbers to 20

## Compare numbers to 20

## Notes and guidance

In this small step, children build on their understanding of comparing numbers from the Autumn term to compare pairs of numbers up to and including 20

Children can use their knowledge of counting to support them. For example, because they say 16 after 15 , they know that 16 is greater than 15 . They can also use their knowledge of representing numbers using objects to help them identify which number in a pair is greater or less than the other. Ten frames and number lines are useful representations to support children when comparing numbers.

Both the inequality symbols and the language of "greater than", "less than" and "equal to" are used throughout. It is important that children see examples of all the symbols, to reinforce their meaning. Children also compare numbers written as words.

## Things to look out for

- Children may think that, for example, 7 is greater than 15 because 7 is greater than 5
- Children may find it more difficult to compare numbers to zero as it is harder to visualise.


## Key questions

- When you count from zero, which of the numbers do you say first?
- Which number is further along the number line?
- Which number is greater? How do you know?
- Which is the smaller number? How do you know?
- What does each symbol mean?
- Can you tell me a number that is less/greater than $\qquad$ ?


## Possible sentence stems

- $\qquad$ is less/greater than $\qquad$
- $\qquad$ is equal to $\qquad$
- $\qquad$ </>/= $\qquad$


## National Curriculum links

- Count to and across 100, forwards and backwards, beginning with zero or 1, or from any given number
- Identify and represent numbers using objects and pictorial representations including the number line, and use the language of: equal to, more than, less than (fewer), most, least


## Compare numbers to 20

## Key learning

- Mo and Kim have each made a number.

- What number has Mo made?
- What number has Kim made?
- Who has made the greater number?

- Circle 13 and 19 on the number line.
- Write less or greater to compare the numbers.

13 is $\qquad$ than 19

19 is $\qquad$ than 13

- Write < or > to compare the numbers.


- Write the missing phrase.

- 11 is $\qquad$ 15
equal to

> - Twenty is
$\qquad$ 0

- 13 is $\qquad$ 9
-12 is $\qquad$ twelve.
- Eleven is $\qquad$ 16
- 10 is
$\qquad$ 20
- Write < , > or = to compare the numbers.



- Jo and Max have some marbles.


Who has more marbles?
How do you know?

## Compare numbers to 20

## Reasoning and problem solving



How many sweets could there be in jar $B$ ?

Compare answers with a partner.

$13,14,15,16$


What could the missing numbers be?


Compare answers with a partner.

Give each child a Rekenrek.
Tell children a number between 0 and 20 and ask them to make a number that is greater/less than your number.

How do they know that it is greater/less?
$16,17,18,19$
$13,14,15,16,17$
multiple possible answers

## Order numbers to 20

## Notes and guidance

Now that children are confident in counting and comparing numbers to 20, in this small step they move on to ordering sets of three numbers.

Expose children to different methods for ordering such as comparing two groups initially and lining groups up. Children should use the language they used in the previous step as well as "greatest", "smallest", "most" and "fewest".
Children need to apply their knowledge of tens and ones to help them work abstractly. For example, when ordering 8, 17 and 14 children should recognise that 8 is the only number that does not have 1 ten, therefore 8 is the smallest of the three numbers.

## Things to look out for

- Children may compare the ones in a number without considering the tens and so think that 8 is greater than 15 , because 8 is greater than 5
- Children may struggle with descending order, and think that numbers can only be ordered from smallest to greatest.


## Key questions

- How did you compare the groups?
- How do you know that group $\qquad$ has the most/fewest?
- How do you know that group $\qquad$ is the greatest/smallest?
- How can you show the numbers using cubes or counters?
- Do you need to start with the smallest or the greatest number?
- Which number is the greatest/smallest? How do you know?
- Do all the numbers have tens? How does this help?


## Possible sentence stems

- $\qquad$ has $\qquad$ ten and $\qquad$ ones.
- $\qquad$ ones is greater/less than $\qquad$ ones, so $\qquad$ is greater/less than $\qquad$
- The greatest/smallest number is $\qquad$


## National Curriculum links

- Identify and represent numbers using objects and pictorial representations including the number line, and use the language of: equal to, more than, less than (fewer), most, least


## Order numbers to 20

## Key learning

- Mo, Max and Kim use counters to make numbers.

- What numbers have they made?
- Who has made the greatest number? How do you know?
- Who has made the smallest number? How do you know?
- Write the numbers in order.

Start with the smallest number.

- Here are three groups of sweets.


Put the groups in order.
Start with the one that has the most sweets.

- Mrs Smith has made three numbers on Rekenreks.

- What numbers has Mrs Smith made?
- Write the numbers in order.

Start with the greatest number.

- Complete the sentences for each set of numbers.
$\qquad$ is the greatest number.
$\qquad$ is the smallest number.
$\square$
$13,18,15$
$20,17,11$
nineteen, zero, fifteen


## Order numbers to 20

## Reasoning and problem solving

Match the labels to the pictures.

$$
15,17,19
$$

## $11,18,13$

$14,12,5$


Order the numbers in each set from smallest to greatest.
Order all the numbers from greatest to smallest.


15, 17, 19
11, 13, 18
$5,12,14$
$5,11,12,13,14,15,17,18,19$

Tiny is making numbers in order from greatest to smallest.
multiple possible answers, e.g.
17, 14, 13
17, 8, 0
Children could also add counters to the first set of ten frames, which gives even more possible answers.

## Spring Block 2

## Addition and subtraction (within 20)

| Step 1 | Add by counting on within 20 |
| :--- | :--- |
| Step 2 | Add ones using number bonds |
| Step 3 | Find and make number bonds to 20 |
| Step 4 | Doubles |
| Step 5 | Near doubles |
| Step 6 | Subtract ones using number bonds |
|  |  |
| Step 7 | Subtraction - counting back |
|  |  |
| Step 8 | Subtraction - finding the difference |

## Small steps

## Add by counting on within 20

## Notes and guidance

In this small step, children build on their learning from earlier in the year as they explore addition by counting on from a given number within 20

The use of ten frames and counters or cubes is particularly useful, together with bar models. Children should begin to understand that addition is commutative (although they do not need to formally know the word), and that it is more efficient to start from the greater number than the smaller number. For example, when working out $1+13$, it is quicker to add 1 to 13 than to add 13 to 1 . A number line is a particularly useful tool to exemplify this point, as children see the benefit of drawing just 1 jump rather than drawing 13 jumps.
It is important that children see that they are not just counting the total of two separate numbers or items; rather, they are adding to what they already have.

## Things to look out for

- Children may count all the items, starting from 1 , rather than counting on from one of the numbers in the addition.
- Children may always start from the first number in the addition, rather than starting from the greater number.


## Key questions

- What number did you start with? Then what happened? Now what do you have?
- Is it quicker to add 4 to 9 or to add 9 to 4 ? Is the answer the same?
- How can you use a number line to count on from $\qquad$ ?
- How do the counters show the question?
- How can you use a bar model or a number line to show counting on?


## Possible sentence stems

- First, I had $\qquad$
Then I counted on $\qquad$
Now I have $\qquad$
- To work out $\qquad$ + $\qquad$ I will count on from $\qquad$


## National Curriculum links

- Read, write and interpret mathematical statements involving addition (+), subtraction (-) and equals (=) signs
- Add and subtract 1-digit and 2-digit numbers to 20, including zero


## Add by counting on within 20

## Key learning

Show children how to play snakes and ladders. Encourage them to count on using the numbers on the board. For example, if they start on 13 and roll a 4, they count " $14,15,16,17$ ".

Put children into groups.
Point to yourself and begin counting. When you point to another group, they continue the count. Keep switching between groups.
Repeat with different starting numbers. This activity is great for creating rhythmical patterns and can be extended to more than one group of children.

Read Mr Gumpy's Outing by John Burningham.
Ask children to build a boat and to create their own "first, then, now" stories as different groups of characters climb aboard. Encourage children to count on as more children join the boat.

- Use ten frames to complete the number story.


First there were $\qquad$ cars in the car park.

Then $\qquad$ more cars parked in the car park.

Now there are $\qquad$ cars in the car park.

- Use the bar model to help you solve the problem.


## Ann has 13 marbles.

She gets 5 more marbles.
How many marbles does Ann have now?
13

- Dan starts at 9 and counts on 6

Show this on the number line and complete the number sentence.

$9+6=$ $\qquad$

## Add by counting on within 20

## Reasoning and problem solving



## Add ones using number bonds

## Notes and guidance

In this small step, children use number bonds and related facts when adding within 20, as an alternative to counting on. This is a more efficient method because, for example, if they know that 4 and 2 are a bond to 6 , they can use this fact to see that 14 and 2 are a bond to 16 , as are 4 and 12

Using counters and ten frames and base 10 enables children to see the links between related facts, noticing that, for example, $11+6$ is 10 more than $1+6$

Children can also explore missing number problems such as $5+$ $\qquad$ $=17$ using the knowledge that 5 and 2 are a number bond to 7

## Things to look out for

- If children are not secure with number bonds within 10 , they may make errors when trying to find the related facts within 20
- Children may not see that they can use a single number bond within 10 to find two different addition facts within 20 , for example using $3+2$ to work out both $13+2$ and $12+3$


## Key questions

- What is the same and what is different about 4 and 14 ?
- If you know that 4 plus 2 is equal to 16 , how can you use this to work out 14 plus 2?
- What do you notice about $14+2$ and $12+4$ ? How many tens are there in each addition? How many ones are there?
- What is the number bond for 5 to 7 ?

How can you use this to help work out $15+$ $\qquad$ $=17$ ? What about $5+$ $\qquad$ $=17$ ?

## Possible sentence stems

- $\qquad$ and $\qquad$ are a number bond to $\qquad$
So $\qquad$ and $\qquad$ are a number bond to $\qquad$
- There are $\qquad$ ones altogether and $\qquad$ ten, so the total is $\qquad$


## National Curriculum links

- Represent and use number bonds and related subtraction facts within 20
- Add and subtract 1-digit and 2-digit numbers to 20 , including zero


## Add ones using number bonds

- Complete the additions.

$4+2=$ $\qquad$

$14+2=$ $\qquad$

$12+4=$ $\qquad$
- Complete the additions.



## Add ones using number bonds

## Reasoning and problem solving

Tiny is working out the missing number.


Do you agree with Tiny?
Why?


Work out the missing numbers.
$1+$ $\qquad$ $=6$ $\qquad$ $+3=9$
$11+$ $\qquad$ $=16$ $\qquad$ $+3=19$

Sam, Max and Mo are working out $5+14$


## Notes and guidance

In this small step, children explore number bonds to 20 . They have already learnt about number bonds to 10 and should be confident with these. It is essential that children are fluent in their number bonds as they are used frequently throughout the curriculum.

Children use their knowledge of number bonds to 10 to find number bonds to 20 . Using examples such as $7+3,17+3$ and $7+13$ encourages children to see the link between bonds to 10 and bonds to 20, as well as reinforcing their understanding of place value. They see that working systematically helps them to find all the possible number bonds to 20
Representations such as ten frames, counters, Rekenreks and part-whole models, among others, can be used to support children's understanding.

## Things to look out for

- Children may add a 10 to both numbers, for example $14+16=20$
- Children may miscalculate if they are using counting on as a strategy for working out the number bond. Using equipment such as ten frames can help with this.


## Key questions

- How many more do you need to make 20?
- How does knowing the number bonds to 10 help you to work out the number bonds to 20 ?
- What is the same and what is different about $4+6=10$ and $14+6=20$ ?
- How do you know that you have found all the number bonds?


## Possible sentence stems

- There are $\qquad$ red counters and $\qquad$ yellow counters.

There are $\qquad$ counters altogether.

This means that $\qquad$ and $\qquad$ are a bond to $\qquad$
$\qquad$ $+$ $\qquad$ $=$ $\qquad$

- I know that $\qquad$ $+$ $\qquad$ $=10$, so $\qquad$ $+$ $\qquad$ $=20$


## National Curriculum links

- Read, write and interpret mathematical statements involving addition (+), subtraction (-) and equals (=) signs
- Represent and use number bonds and related subtraction facts within 20


## Find and make number bonds to 20

## Key learning

Provide pots labelled with numbers 1-20 and a selection of natural objects.
Ask children to count the correct number of items into each pot.

Can they find 2 pots that have 20 items in total?
Is there more than one way to do it?
Ask children to draw what they have found.

Chalk two large ten frames onto the playground. Tell the children you have hidden 20 beanbags and that they need to find them!
As the children find the beanbags, they put them into the ten frames.

Prompt children to use the ten frames to help them see how many they have found and how many are still hidden.


- Complete the sentences for each picture.


There are $\qquad$ red counters.

There are $\qquad$ yellow counters.

There are $\qquad$ counters altogether.
$\qquad$ $+$ $\qquad$ $=$

- Continue the pattern to find all the number bonds to 20

$$
\begin{aligned}
& 20=20+0 \\
& 20=19+1 \\
& 20=18+2 \\
& 20=17+3
\end{aligned}
$$

How do you know that you have found them all?

## Reasoning and problem solving

Use counters to show each addition.

$$
7+3=10
$$

$$
17+3=20
$$

$$
20=7+13
$$

What is the same?
What is different?
Talk about it with a partner.

Kay shows a number bond to 20 in a part-whole model.


What mistake has Kay made?


## Key questions

- How can you sort these pictures into doubles and not doubles?
- How do you know that this shows a double?
- How can you make double $\qquad$ ?
- How can you show the double differently?
- If double 2 is 4 , what do you think double 3 is?
- What is the greatest double you can roll on a normal dice?
- What is 12 the double of?


## Possible sentence stems

- $\qquad$ $+$ $\qquad$ $=$ $\qquad$ , so double $\qquad$ is $\qquad$

Double $\qquad$ is $\qquad$

- $\qquad$ is the double of $\qquad$


## National Curriculum links

- Read, write and interpret mathematical statements involving addition ( + ), subtraction ( - ) and equals ( $=$ ) signs
- Add and subtract 1-digit and 2-digit numbers to 20 , including zero


## Doubles

## Key learning

Read Double the Ducks by Stuart J. Murphy.
In groups, ask children to think of their own doubling story and act it out. You could give each group the following starting point.

A farm has 3 horses, 4 sheep, 7 cows and 1 goat.

Tell children to take turns rolling two dice. They score a point each time they roll a double. The first to reach 3 points wins the game.


Hide number pieces outside.
Give each child a number piece. Ask them to find another one that is the same to make a double. Ask them to say the double they have found, for example "Double 5 is 10 "


- Which pictures show doubles?

- Draw counters to work out the doubles.


Double 5 is $\qquad$


Double 7 is

100000


## Doubles

## Reasoning and problem solving



## Near doubles

## Notes and guidance

Building on the previous step, in this small step children use doubles to help work out near doubles. For example, they can use the double fact that $6+6=12$ to work out $6+7$ by adding 1 more. They should see that this is a more efficient method than counting on.

As in the previous step, building numbers in a pair-wise pattern on ten frames can help children visualise that to work out $3+4$, they can do $3+3$ plus 1 more.

Children can also explore finding near doubles through subtraction, for example $3+4$ is equal to $4+4$ minus 1 . This can be useful for children who are more confident with certain doubles than others. For example, if a child is not confident with doubling 7 , they may struggle with $7+8$, but if they can double 8 , they can use this fact instead.

## Things to look out for

- Children may be more confident with doubles less than 10 , such as double 4 , and require extra support with doubles that go beyond 10
- Children may not be able to quickly recall 1 more or 1 less than any number within 20


## Key questions

- What does double $\qquad$ mean?
- What is double $\qquad$ ?
- What is 1 more than $\qquad$ ?
- If $\qquad$ is 1 more than $\qquad$ how can you use this to work out $\qquad$ $+$ $\qquad$ ?
- $\qquad$ is 1 less than $\qquad$ how can you use this to work
out $\qquad$ $+$ $\qquad$ ?


## Possible sentence stems

- $\qquad$ is 1 more than $\qquad$ so I can work out double $\qquad$ and then add 1
- Double $\qquad$ plus 1 is equal to $\qquad$
is 1 less than $\qquad$ , so I can work out double $\qquad$ and then subtract 1


## National Curriculum links

- Add and subtract 1-digit and 2-digit numbers to 20, including zero


## Near doubles

## Key learning

Draw a number track from 0 to 20 in chalk on the playground. Only show the even numbers.


Ask children to stand on a number and then to write either 1 more or 1 less than their number in the adjacent box.

- What additions are shown?

$\qquad$ $+$ $\qquad$

$\qquad$ $+$ $\qquad$
- What do you notice about the number of red counters in each ten frame?
- What do you notice about the number of yellow counters in each ten frame?
- What do you notice about the total number of counters in each ten frame?
- What double is shown on the ten frame?


Add one more red counter to the ten frame.
What addition is shown now?
Complete the sentence.
$\qquad$ $+$ $\qquad$ is equal to double $\qquad$ plus 1

- Use the counters and ten frames to complete the sentence.

$6+7=$ double $\qquad$ plus $\qquad$
- Use counters and ten frames to show that:

$$
2+3=\text { double } 2 \text { plus } 1 \quad 9+8=\text { double } 8 \text { plus } 1
$$

- Use doubles to work out the near doubles.

$$
8+7
$$

$$
5+4
$$

$$
9+8
$$

## Near doubles

## Reasoning and problem solving

Tiny uses doubles to work out $5+4$


 double 8

What mistake has Tiny made?
What is the correct answer?

Write < , > or = to complete the number sentences.

double 9
 $9+8$

9

$<$
$>$
$>$

Sam and Max are working out $8+7$


How can Sam use this fact to work out $8+7$ ?


How can Max use this fact to work out $8+7$ ?

Use counters to help you.
add 1
subtract 1

## Subtract ones using number bonds

## Notes and guidance

In this small step, children begin subtracting within 20. Earlier in the year, children subtracted within 10 by counting back and using number lines. They now subtract within 20 using their knowledge of number bonds. For example, if they know the number bond $7-5=2$, then they know that 17-5 $=12$

By completing these calculations side by side using ten frames, counters, part-whole models or base 10, children see that the second subtraction will have an answer that is 10 greater than the first subtraction.

At this stage, none of the subtractions cross 10, so children can focus on using their number bond knowledge rather than counting back, which is covered in the next step.

## Things to look out for

- Children may be unsure of the number bond facts within 10
- Children may not see the link between 4-1=3 and $14-1=13$
- Children may incorrectly use their number bond knowledge, for example 14-1 = 3


## Key questions

- What are $\qquad$ and $\qquad$ a number bond to?
- What is the same and what is different about 5 and 15 ?
- If you know that 7 subtract 2 is equal to 5 , how can you use this to work out 17-2?
- What do you notice about 17-2 and 17-4? How many tens are there in each subtraction? How many ones are there?
- What is the number bond for 5 to 8 ? How can you use this to help work out $18-5$ ?


## Possible sentence stems

- The number bond for $\qquad$ to $\qquad$ is $\qquad$ So the number bond for $\qquad$ to $\qquad$ is $\qquad$
- There will be $\qquad$ ones and $\qquad$ ten, so the answer is $\qquad$


## National Curriculum links

- Represent and use number bonds and related subtraction facts within 20
- Add and subtract 1 -digit and 2 -digit numbers to 20 , including zero


## Subtract ones using number bonds

## Key learning

Draw two number tracks on the playground.


Ask one child to stand on 10 and another on 20 Roll a dice and ask both children to hop back along their track the number rolled. What do they notice about where they have landed?
Repeat for other starting numbers, ensuring that the answer does not go below 0 or 10, respectively.

Provide pairs of children with three ten frames and some counters. Ask one child to make a number between 6 and 10 and the other to make the number that is 10 more.
Roll a dice and ask each child to subtract the counters from their ten frames. What do they notice about their answers?
Ask them to write number sentences that match their subtractions.

- Complete the subtractions.


$$
8-3=
$$


$18-3=$ $\qquad$

- Complete the part-whole models.


Write a subtraction number sentence for each part-whole model. What do you notice?

- Use number bonds to work out the subtractions.



## Subtract ones using number bonds

## Reasoning and problem solving



## Subtraction - counting back

## Notes and guidance

In this small step, children build on the language of subtraction, recognising the subtraction symbol from earlier learning and using it within 20

Children use the counting back strategy for numbers within 20 , including subtractions that cross 10 . The use of zero is important, so children know that when nothing is taken away, the start number remains the same, or when the whole group is taken away, there will be nothing left. Crossing out and using a number line are particularly useful for counting back to work out subtractions.

This can also be linked with "first, then, now" stories.

## Things to look out for

- When counting back, children may include the start number. For example, when working out $15-4$, they may count "15, 14, 13, 12".
- Children may write calculations the wrong way around if they do not understand the importance of order when subtracting, thinking that it is the same as addition, where the order does not matter. For example, they may write 4-15 but still give the answer 11


## Key questions

- How many objects were there at first?

Then what happened to the objects? How many objects are there now?

- How does using counters help you?
- How does using a number line help you?
- Can you think of another way to show the problem?


## Possible sentence stems

- First there were $\qquad$
Then $\qquad$ were taken away.

Now, there are $\qquad$

- $\qquad$ subtract $\qquad$ is equal to $\qquad$


## National Curriculum links

- Read, write and interpret mathematical statements involving addition ( + ), subtraction ( - ) and equals ( $=$ ) signs
- Add and subtract 1-digit and 2-digit numbers to 20 , including zero


## Subtraction - counting back

- First there were 14 sheep.

Then they all ran away.
How many sheep are left?
Use ten frames and counters to work it out.
Complete the number sentence.
$\qquad$ - $\qquad$ $=$ $\qquad$

- Tiny has 13 stars for being helpful!


Tiny gives 4 stars to Fay.
How many stars does Tiny have left?

- Max uses a number line to work out 20 - 7


Use a number line to work out the subtractions.

- 20-8
- 18-9
- 19-4


## Subtraction - counting back

## Reasoning and problem solving



Mo

Write < , > or = to make the statements correct.


## Notes and guidance

In this small step, children formally learn about finding the difference for the first time and explore it as a form of subtraction.

Children often struggle with this concept as they are not required to physically take away or count back a specified amount as they have previously experienced. Instead, they are making comparisons between two amounts. In some cases the question will be worded as "How many more ...?" Up until now, they have only encountered the word "more" when thinking about addition.

Children can use their skills of counting back and counting on to help them find the difference. Alternatively, they can make both amounts and visually see how many more or less a number is.

## Things to look out for

- Children may add instead of subtracting.
- Children may include the start number when counting back.
- Children may misinterpret the word "difference" in a mathematical context, for example describing the difference in appearance of the numbers.


## Key questions

- Who has more? How do you know? How many more does
$\qquad$ have?
- What does "difference" mean?
- What strategy can you use to find the difference?
- What pictures/objects can you use to show this?
- How can you complete the sentences?
- How do the counters/bar models help you to subtract?
- Which method will you use to show your thinking? Why?
- Did you count forwards or backwards? Why?


## Possible sentence stems

- The difference between $\qquad$ and $\qquad$ is $\qquad$
- When finding the difference, I can ...
- $\qquad$ is the difference between $\qquad$ and $\qquad$


## National Curriculum links

- Read, write and interpret mathematical statements involving addition ( + ), subtraction ( - ) and equals ( $=$ ) signs
- Add and subtract 1-digit and 2-digit numbers to 20 , including zero


## Subtraction - finding the difference

## Key learning

Take the class into the playground. Ask the boys and the girls to stand in separate lines next to each other. Make sure they are lined up in pairs.
Ask what the difference is between the number of boys and the number of girls?

Repeat the activity with different criteria, for example children collecting either sticks or pebbles.

- How many more cakes does Sam have than Max?


Max


Sam has $\qquad$ more cakes than Max.

- Kim has 7 sweets and Mo has 3 sweets.


How many more sweets does Kim have than Mo? How many fewer sweets does Mo have than Kim?

- Ann has 13 marbles.

Tom has 5 marbles.


How many more marbles does Ann have than Tom?

## Subtraction - finding the difference

## Reasoning and problem solving

Two numbers have a difference of 4
The greater number is less than 15
The smaller number is more than 6
What could the two numbers be?


14 and 10,13 and 9 ,
12 and 8,11 and 7
multiple possible answers

There are 11 pink pens and 7 green pens in a pot.
How many more pink pens are there than green pens?


What mistake has Tiny made?
Draw a picture to show the correct answer.


Tiny has added the numbers instead of subtracting them.

## Related facts

## Notes and guidance

Now that children have spent some time exploring addition and subtraction separately, in this small step they look at how they relate to each other, considering the addition and subtraction fact families for numbers within 20

Children use both concrete resources and pictures to find links between the addition and subtraction sentences. Highlight that addition and subtraction are inverse operations. As well as finding the four related facts, children can write the sentences with the " $=$ " at either the end or the start.

Throughout this step, the idea of commutativity should be reinforced, and children should be able to verbalise that addition can be done in any order, whereas subtraction cannot. It is not necessary for children to use the word "commutative" at this stage.

## Things to look out for

- Children may work out subtractions correctly, but write them incorrectly, for example 7-12=5
- Children may think that by writing " $=$ " in a different place they have written a different fact, for example $3+5=8$ and $3=5+8$


## Key questions

- What is the same and what is different?
- What addition sentences can you write? What subtraction sentences can you write? Can you write any of them another way?
- If you know that $12+1=13$, what else do you know?
- Can you see any patterns?
- If you know that $15-3=12$, why can you not say $3-15=12$ ? Use counters to show this.


## Possible sentence stems

- $\qquad$ can be done in any order.
- $\qquad$ cannot be done in any order.
- If I know that $\qquad$ $+$ $\qquad$ $=$ $\qquad$ then I also know that
$\qquad$ - $\qquad$ $=$ $\qquad$


## National Curriculum links

- Represent and use number bonds and related subtraction facts within 20
- Add and subtract 1-digit and 2-digit numbers to 20, including zero


## Related facts

## Key learning

- Complete the addition and subtraction sentences for each picture.

$12+1=$ $\qquad$
$13-1=$ $\qquad$

$11+$ $\qquad$ $=13$

$13-$ $\qquad$ $=$ $\qquad$
$+$ $\qquad$ $=18$
$\qquad$ $+$ $=18$

18 - $\qquad$ $=$ $\qquad$
18 - $\qquad$ = $\qquad$
$=$ $\qquad$ - $\qquad$ $=$
$\qquad$ $=$ $\qquad$ - $\qquad$

- Complete the bar models.

| 17 |  |
| :--- | :--- |
|  | 6 |



Write the fact family for each bar model.
Use the numbers 8, 7 and 15 to draw your own bar model. Write the fact family for your bar model.

## Related facts

## Reasoning and problem solving



Which number sentences match the ten frames?


How do you know?


$$
\begin{aligned}
& 15+3=18 \\
& 18-15=3 \\
& 18-3=15 \\
& 18=3+15
\end{aligned}
$$

## Notes and guidance

In this final small step, children explore missing number problems. They use the idea of inverse operations to see that if they start with a number and add 2 to it, then to "undo" that they need to subtract 2. Bar models and part-whole models are useful representations for this.
"First, then, now" stories can be particularly helpful for children to act out the problems and visualise what is happening. Use of counters and ten frames, as well as number lines, supports children in their understanding of a missing number problem, helping them to discuss what the numbers in a problem represent.

With the missing number problem $3+$ $\qquad$ = 5, a common mistake is to add 3 and 5 and get $3+8=5$. Children need to spot that this does not make sense, as 8 is greater than 5

## Things to look out for

- Children may just look at the numbers and operation rather than thinking about the missing number element of the problem.
- Children may find it more challenging when number sentences are written in the form $4=$ $\qquad$ - 2 rather than $\qquad$ $-2=4$


## Key questions

- If I add/subtract $\qquad$ counters to/from the ten frame, how can you undo what I have done?
- How many counters do you need to add to/subtract from
$\qquad$ to get $\qquad$
- If you know the whole and a part, how can you find the other part?
- Should the missing number be greater than or less than $\qquad$ ? How do you know?


## Possible sentence stems

- First there were ...

Then ...
Now there are ..

- If $\qquad$ is the whole and $\qquad$ is a part, then the other part must be $\qquad$


## National Curriculum links

- Solve one-step problems that involve addition and subtraction, using concrete objects and pictorial representations, and missing number problems such as $7=$ ? -9


## Missing number problems

## Key learning

Give children 8 counters and a ten frame. Ask them to act out the "first, then, now" stories.

First there were 3 frogs in the pond. Then some more frogs jumped into the pond.

Now there are 8 frogs in the pond.
How many frogs jumped into the pond?

First there were 8 children sitting at the table.
Then some children went away.
Now there are 6 children sitting at the table.
How many children went away?
-
First there were 12 birds in a tree.
Then some of the birds flew away.
Now there are 10 birds in the tree.

How many birds flew away?
$12-$ $\qquad$ $=10$

- Complete the part-whole models and number sentences.

$4+$ $\qquad$ $=6$

$\qquad$ $+5=12$
- Use the number lines to find the missing numbers.
- $3+$ $\qquad$ $=12$

- $11-\quad=8$



## Missing number problems

## Reasoning and problem solving

Jo is working out the missing number.


What mistake has Jo made?
What is the missing number?


Max and Sam are working out the missing number.


Sam draws a number line to help.


Who do you agree with?
Why?

