## Autumn

Scheme of learning

## Year 4

## The White Rose Maths schemes of learning

## Teaching for mastery

Our research-based schemes of learning are designed to support a mastery approach to teaching and learning and are consistent with the aims and objectives of the National Curriculum.

## Putting number first

Our schemes have number at their heart.
A significant amount of time is spent reinforcing number in order to build competency and ensure children can confidently access the rest of the curriculum.

## Depth before breadth

Our easy-to-follow schemes support teachers to stay within the required key stage so that children acquire depth of knowledge in each topic. Opportunities to revisit previously learned skills are built into later blocks.

## Working together

Children can progress through the schemes as a whole group, encouraging students of all abilities to support each other in their learning.

Fluency, reasoning and problem solving
Our schemes develop all three key areas of the National Curriculum, giving children the knowledge and skills they need to become confident mathematicians.

## Concrete - Pictorial - Abstract (CPA)

Research shows that all children, when introduced to a new concept, should have the opportunity to build competency by following the CPA approach. This features throughout our schemes of learning.

## Concrete

Children should have the opportunity to work with physical objects/concrete resources, in order to bring the maths to life and to build understanding of what they are doing.


## Pictorial

Alongside concrete resources, children should work with pictorial representations, making links to the concrete. Visualising a problem in this way can

$\square$ help children to reason and to solve problems.

Abstract
With the support of both the concrete and pictorial representations, children can develop their $5+7$ understanding of abstract methods.

If you have questions about this approach and would like to consider appropriate CPD, please visit www.whiterosemaths.com to find a course that's right for you.

## Teacher guidance

Every block in our schemes of learning is broken down into manageable small steps, and we provide comprehensive teacher guidance for each one. Here are the features included in each step.
 being addressed by the step.

## Teacher guidance

A Key learning section, which provides plenty of exemplar questions that can be used when teaching the topic.


Reasoning and problem-solving activities and questions that can be used in class to provide further challenge and to encourage deeper understanding of each topic.


Answers provided where appropriate

## Activities and symbols

## Key Stage 1 activities

Key Stage 1 includes more hands-on activities alongside questions.


## Key Stage 1 and 2 symbols

The following symbols are used to indicate:

concrete resources might be useful to help answer the question

a bar model might be useful to help answer the question

drawing a picture might help children to answer the question
children talk about and compare their answers and reasoning
a question that should really make children think. The question may be structured differently or require a different approach from others and/or tease out common misconceptions.

## Free supporting materials

End-of-block assessments to check progress and identify gaps in knowledge and understanding.


Each small step has an accompanying home learning video where one of our team of specialists models the learning in the step. These can also be used to support students who are absent or who need to catch up content from earlier blocks or years.



End-of-term assessments for a more summative view of where children are succeeding and where they may need more support.

## Free supporting materials



## Premium supporting materials



## Premium supporting materials

Teaching slides that mirror the content of our home learning videos for each step. These are fully animated and editable, so can be adapted to the needs of any class.


## A true or false

 question for every small step in the scheme of learning. These can be used to support new learning or as another tool for revisiting knowledge at a later date.Flashback 4 starter activities
to improve retention.
Q1 is from the last lesson;
Q2 is from last week;
Q3 is from 2 to 3 weeks ago;
Q4 is from last term/year.
There is also a bonus question on each one to recap topics such as telling the time,
times-tables and Roman numerals.


Topic-based CPD videos
As part of our on-demand CPD package,
our maths specialists provide helpful hints and guidance on teaching topics for every block in our schemes of learning.

## Meet the characters

Our class of characters bring the schemes to life, and will be sure to engage learners of all ages and abilities. Follow the children and their class pet, Tiny the tortoise, as they explore new mathematical concepts and ideas.


Yearly overview
The yearly overview provides suggested timings for each block of learning, which can be adapted to suit different term dates or other requirements.


Autumn Block 1 Place value

## Small steps

| Step 1 | Represent numbers to 1,000 |
| :--- | :--- |
| Step 2 | Partition numbers to 1,000 |
| Step 3 | Number line to 1,000 |
| Step 4 | Thousands |
| Step 5 | Represent numbers to 10,000 |
| Step 6 | Partition numbers to 10,000 |
| Step 7 | Flexible partitioning of numbers to 10,000 |
|  |  |
| Step 8 | Find 1, 10, 100, 1,000 more or less |

## Small steps

| Step 9 | Number line to 10,000 |
| :--- | :--- |
|  | Estimate on a number line to 10,000 |
| Step 11 | Compare numbers to 10,000 |
| Step 12 | Order numbers to 10,000 |
| Step 13 | Roman numerals |
|  |  |
| Step 14 | Round to the nearest 10 |
|  |  |
| Step 15 | Round to the nearest 100 |
|  |  |
| Step 16 | Round to the nearest 1,000 |

## Small steps

## Represent numbers to 1,000

## Notes and guidance

Children learned how to represent numbers to 1,000 in Year 3 a concept that will be reinforced in this small step to ensure they have a sound understanding. This understanding will be important later in the block, as children begin to explore numbers over 1,000

Examples have been chosen to ensure that children look at representing and interpreting numbers that have no tens or no ones, to reinforce the idea of using zero as a placeholder. Base 10 and place value counters are used throughout. Base 10 can help children understand the size of a number, while place value counters are more efficient later in the block, when working with 4-digit numbers.

## Things to look out for

- Children may write numbers incorrectly, for example 421 as 400201
- Children may not understand the place value of each digit in a number.
- Children may not use placeholders appropriately.
- Children may not recognise the value of a place value counter correctly, because different place value counters are identical in size.


## Key questions

- What is the value of each base 10 piece?
- What is the value of each place value counter?
- How did you count the pieces?
- Does the order in which you build the number matter?
- Can you represent the number another way?
- What do you do if there are no tens?


## Possible sentence stems

- There are $\qquad$ hundreds, $\qquad$ tens and $\qquad$ ones.

The number is $\qquad$

- When a number has no $\qquad$ then we use $\qquad$ as a placeholder.


## National Curriculum links

- Read and write numbers up to 1,000 in numerals and words (Y3)
- Identify, represent and estimate numbers using different representations


## Represent numbers to 1,000

## Key learning

- How many candles are there?


Write your answer in numerals and words.

- What numbers are represented?

- Use base 10 to represent each number.

- Annie is drawing place value counters to represent 516
- What numbers are represented?

(100) 100 (100) (100)



#### Abstract

Complete her drawing.


(1)

## Represent numbers to 1,000

## Reasoning and problem solving

Whitney and Dexter have each made a number.


What numbers have they made?
What is the same about
their numbers?
What is different?

Whitney and Dexter have both made the number 231

## Notes and guidance

In this small step, children partition numbers up to 1,000 into hundreds, tens and ones.

Children represent numbers in a part-whole model and identify missing parts and wholes. They write numbers in expanded form, using the part-whole model as support where needed, and identify the number of hundreds, tens and ones in a 3 -digit number. Particular attention should be paid to numbers that include zero as a placeholder, to build on learning from the previous step.

Base 10 and place value counters can continue to be used to support children's understanding.

## Things to look out for

- Children may not correctly assign place value to each digit of a number. For example, they may write $423=4+2+3$
- Children may not recognise a number represented by a part-whole model, where the parts are not given in value order.
- Children may say that 423 has 20 tens rather than 2 tens, because they confuse place value language.


## Key questions

- How many hundreds/tens/ones are there in 465?
- How do you write a number that has zero tens?
- How do you write a number that has zero ones?
- What number is equal to $300+70+9$ ?
- What is the value of the missing part? How do you know?
- What is the value of the digit $\qquad$ in the number $\qquad$ ?


## Possible sentence stems

- $\qquad$ has $\qquad$ hundreds, $\qquad$ tens and $\qquad$ ones.
$\qquad$ = $\qquad$ $+$ $\qquad$ $+$ $\qquad$
- The number that is made up of $\qquad$ hundreds, $\qquad$ tens and $\qquad$ ones is $\qquad$


## National Curriculum links

- Identify, represent and estimate numbers using different representations
- Recognise the place value of each digit in a 3-digit number (hundreds, tens, ones) (Y3)


## Partition numbers to 1,000

## Key learning

- Use the base 10 to help you complete the number sentences.

$451=400+$ $\qquad$ $+$ $\qquad$

$347=$ $\qquad$ $+$ $\qquad$ $+$ $\qquad$

$265=$ $\qquad$ $+$ $\qquad$ $+$ $\qquad$
- Complete the number sentences.
- 982 = $\qquad$ $+$ $\qquad$ $+$ $\qquad$
- $980=$ $\qquad$
$\qquad$
- $902=$ $\qquad$ $+$ $\qquad$
- Complete the part-whole models.

- Complete the sentences.
- 259 has $\qquad$ hundreds, $\qquad$ tens and $\qquad$ ones.
- 813 has 8 $\qquad$ , 1 $\qquad$ and 3 $\qquad$
- 106 has $\qquad$ hundred $\qquad$ tens and $\qquad$ ones.
- $\qquad$ has 5 hundreds, 1 ten and 0 ones.
- How many hundreds does the number 907 have? How many ones does the number 36 have? How many tens does the number 680 have?
- Write in numerals the number that has 7 hundreds, 1 one and 2 tens.


## Partition numbers to 1,000

## Reasoning and problem solving



Explain the mistake that Tiny has made.

What is the whole?

Dexter is thinking of a number.


What could Dexter's number be?
Find each possibility and partition it.

$$
\begin{aligned}
& 244=200+40+4 \\
& 433=400+30+3 \\
& 622=600+20+2 \\
& 811=800+10+1
\end{aligned}
$$

## Notes and guidance

In this small step, children revisit the number line to 1,000 , which they were first introduced to in Year 3

Children label, identify and find missing values on blank or partially completed number lines. Using real-life scales, such as rulers and measuring jugs, can be helpful here.
When looking at partially completed number lines, it is important that children become confident in finding the difference between the start and end points and dividing to find the value of each interval. Explicit examples should be used that have a varying number of intervals and unmarked values in different positions. Children also learn how to work out the value at the midpoint of an interval.

## Things to look out for

- Children may count the number of divisions, rather than the intervals.
- Support may be needed to work out the midpoint of an interval.
- Children may assume the increments on the number line are each worth one unit, focusing solely on the starting number.


## Key questions

- What are the values at the start and end points of the number line?
- What is the difference in value between the start and end points?
- How many intervals are there?
- How can you work out what each interval is worth?
- How can you work out the halfway point of an interval?
- What other numbers can you mark on the number line?
- Why are the start and end values of a number line important?


## Possible sentence stems

- The difference in value between the start and end of the number line is $\qquad$
- There are $\qquad$ intervals. Each interval is worth $\qquad$


## National Curriculum links

- Identify, represent and estimate numbers using different representations


## Number line to 1,000

## Key learning

- What numbers are the arrows pointing to?

- Complete the sentences for each number line.

Label the number lines.


The difference in value between the start and the end of the number line is $\qquad$ -

There are $\qquad$ intervals.
$\qquad$ $\div$ $\qquad$ $-=$ $\qquad$

- Label 200 and 750 on the number line.

- Label 680 on the number line.

- Draw an arrow to show the position of 550 on each number line.


What do you notice?

## Reasoning and problem solving



No

Filip has poured some juice from a jug.


Estimate how much juice is left in the jug.
approximately
125 ml

## Notes and guidance

Building on previous steps where children explored numbers up to 1,000, they now explore numbers beyond 1,000
The initial focus of this small step is counting in 1,000 s forwards and backwards from any given multiple of 1,000. Number tracks can be used to support this.
Children then look at the composition of multiples of 1,000 by exploring how many hundreds they are made of. They unitise the hundred, being able to state the number of hundreds that make up any 4 -digit multiple of 100 or 1,000 such as " 20 hundreds are equal to 2,000 "
Base 10 and place value counters in a ten frame are helpful when identifying the connection between the number of hundreds that are equal to a multiple of a thousand.

## Things to look out for

- Children may not appreciate that 1,000 is 10 times the size of 100
- When they are meant to be counting in 1,000 s, children may count in the more familiar 100s.
- Children may not use placeholders appropriately.


## Key questions

- Counting in 1,000 s from 3,000, what is the next number?
- Counting back in 1,000 s from 7,000 , tell me a number you would say. How do you know?
- How many thousands are there in 6,000?
- How many hundreds are there in 1,000 ?
- How many hundreds are there in 6,000 ?


## Possible sentence stems

- The next multiple of 1,000 is $\qquad$
- The previous multiple of 1,000 is $\qquad$
- 1 thousand is equal to $\qquad$ hundreds, so
$\qquad$ thousands is equal to $\qquad$ hundreds.
- $\qquad$ thousands can be written in numerals as $\qquad$


## National Curriculum links

- Count in multiples of 6, 7, 9, 25 and 1,000


## Thousands

## Key learning

- How many nails are there?


Write your answer in numerals and words.

- What numbers are represented?

- Complete the number tracks.

| 1,000 | 2,000 |  |  |  |
| :--- | :--- | :--- | :--- | :--- |


|  |  | 7,000 | 8,000 | 9,000 |
| :--- | :--- | :--- | :--- | :--- |

- Complete the sentences.
- There are $\qquad$ ones in a thousand.目

- There are $\qquad$ hundreds in a thousand.
- There are $\qquad$ tens in a thousand.
- Complete the sentences to match the ten frames.

- Complete the sentences.
- 3 thousand $=3,000$

There are $\qquad$ hundreds in 3 thousand.
$>\ldots$ thousand $=5,000$
There are 50 hundreds in $\qquad$ thousand.

## Thousands

## Reasoning and problem solving



What mistake has Tiny made?


Tiny has counted back in 100 s, not 1,000s.

Tiny should say, " $8,000,7,000$,
6,000 ..."

Jack, Huan and Dani are asked to represent 3,000

## Jack



Huan


Who do you agree with?
Explain your answer.

Huan and Dani

## Represent numbers to 10,000

## Notes and guidance

Building on earlier work, where children looked at numbers to 1,000, this small step focuses on representing numbers to 10,000

Children use different representations such as place value charts and Gattegno charts, which highlight the place value of the digits in the numbers. It is important that children explore the relationship "both ways" between the place value columns, for example, 100 is 10 times the size of 10 and a tenth the size of 1,000

It may be helpful to discuss with children how and why we use a comma when writing numbers, as it can help with reading and writing larger numbers.
Children should experience questions that include zero as a placeholder to represent a blank column in a place value chart.

## Things to look out for

- Numbers may be written incorrectly, for example 2,342 as 2000300402
- When using blank counters on a place value chart, children may not make the connection between the column and the value of the counter.
- Children may forget to use zero as a placeholder.


## Key questions

- What number is represented?
- What is the value of each digit?
- Represent 4,672 using base 10/place value counters. How many thousands, hundreds, tens and ones are in the number?
- How would you represent $6,000+0+60+9$ in the place value chart?
- How do you know the counter in the thousands column has a greater value than the counter in the ones column?


## Possible sentence stems

- There are $\qquad$ thousands, $\qquad$ hundreds, $\qquad$ tens and $\qquad$ ones.

The number is $\qquad$

## National Curriculum links

- Recognise the place value of each digit in a 4-digit number (thousands, hundreds, tens and ones)
- Identify, represent and estimate numbers using different representations


## Represent numbers to 10,000

## Key learning

- Complete the sentences.


There are $\qquad$ thousands, $\qquad$ hundreds, $\qquad$ tens and
$\qquad$ ones.

The number is $\qquad$ -

- Use base 10 to represent each number.


## 1,222

1,871

- Complete the sentences.


There are $\qquad$ thousands, $\qquad$ hundreds, $\qquad$ tens and
$\qquad$ ones.

The number is $\qquad$ -

- What numbers are represented on the place value charts?


Write your answers in words and numerals.
What is the same and what is different about the place value charts?

- Use plain counters to represent each number on a place value chart.
- Complete the Gattegno chart to represent the number 5,326

| 1,000 | 2,000 | 3,000 | 4,000 | 5,000 | 6,000 | 7,000 | 8,000 | 9,000 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 100 | 200 | 300 | 400 | 500 | 600 | 700 | 800 | 900 |
| 10 | 20 | 30 | 40 | 50 | 60 | 70 | 80 | 90 |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |

## Represent numbers to 10,000

## Reasoning and problem solving

Aisha is making 3,512 with place value counters.


What other place value counters could she add to make 3,512?

Jack has two 1,000 counters and three 100 counters.
(1.000)
1.000

100


What 4-digit numbers can he make?

Use exactly four counters to make as many 4-digit numbers as possible.

Write each number in numerals.


4,000, 3,100,
3,010, 3,001,
2,200, 2,020,
2,002, 2,110,
2,101, 2,011,
1,300, 1,030,
1,003, 1,210,
1,201, 1,120,
1,102, 1,111

## Notes and guidance

The focus of this small step is to ensure that children have a secure understanding of place value with 4-digit numbers.
Children partition a number up to 10,000 by identifying the number of thousands, hundreds, tens and ones. They should give their answers using numerals, words and expanded form, for example 5,346 $=5$ thousands, 3 hundreds, 4 tens and 6 ones or $5,000+300+40+6$

The familiar representations used earlier in the block can help children to understand the value of each digit. A part-whole model can also support children in partitioning numbers.
Children should experience questions that include zero as a placeholder, so they understand this cannot be omitted, minimising the misconception that $5,006=56$

## Things to look out for

- Children may not associate the digits with their value and just write, for example, 7,645 $=7+6+4+5$
- Partitioned numbers that are presented "out of order" may lead to errors, for example $7,000+3+20+700=7,327$
- Children may omit zero as a placeholder.


## Key questions

- What number is represented?
- How many thousands/hundreds/tens/ones are there in the number $\qquad$ —?
- What is the value of each digit in 4,715 ?
- Does the order in which you partition the number matter?
- What number is equal to $7,000+0+30+4$ ?
- What does a zero in a place value column tell you?


## Possible sentence stems

Possible sentence stems
$\qquad$ has $\qquad$ thousands, $\qquad$ hundreds, $\qquad$ tens and $\qquad$ ones.
$\qquad$ $=$ $\qquad$ $+$ $\qquad$ $+$ $\qquad$ $+$ $\qquad$

## National Curriculum links

- Recognise the place value of each digit in a 4-digit number (thousands, hundreds, tens and ones)
- Identify, represent and estimate numbers using different representations


## Partition numbers to 10,000

## Key learning

- Complete the number sentence.

$3,437=3,000+$ $\qquad$ $+$ $\qquad$ $+$ $\qquad$
- Complete the number sentences.

| Thousands | Hundreds | Tens | Ones |
| :--- | :---: | :--- | :--- |
|  | (100) (100) | $(10)$ | $(1)(1)$ |

$3,412=$ $\qquad$ $+$ $\qquad$ $+$ $\qquad$ $+$ $\qquad$

$\qquad$
$\qquad$ $+$ $\qquad$ $+$ $\qquad$ $+$ $\qquad$

- Use the Gattegno chart to complete the number sentences.

| 1,000 | 2,000 | 3,000 | 4,000 | 5,000 | 6,000 | 7,000 | 8,000 | 9,000 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 100 | 200 | 300 | 400 | 500 | 600 | 700 | 800 | 900 |
| 10 | 20 | 30 | 40 | 50 | 60 | 70 | 80 | 90 |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |

There are $\qquad$ thousands, $\qquad$ hundreds, $\qquad$ tens and
$\qquad$ ones.

The number is $\qquad$

- Complete the part-whole models.

- Complete the sentences.
- 7,812 is equal to $\qquad$ thousands, $\qquad$ hundreds, $\qquad$ tens and $\qquad$ ones.
$\triangleright$ _ is equal to 3 thousands, 4 hundreds, 0 tens and 9 ones.

$$
>\quad=8,000+40+3
$$

## Partition numbers to 10,000

## Reasoning and problem solving

Tiny is partitioning 6,902

$$
6,902=600+90+2
$$

Explain the mistake Tiny has made.

Tiny is partitioning the number 5,232 and representing it in a part-whole model.


Has Tiny partitioned the number correctly?

Explain your answer.

Tiny has not assigned the correct value to each digit because there are no tens.

## Yes

The order of the parts does not matter, as long as they have the correct value.


Use the clues to work out
Tommy's number.

- The thousands digit is $\mathbf{3}$ greater than the tens digit.
- The total sum of digits is $\mathbf{1 6}$
- The 4-digit number is odd.
- The tens digit is 2
- The hundreds digit is double the ones digit.

Think of another 4-digit number and challenge a partner to work out your number from clues.

## Flexible partitioning of numbers to 10,000

## Notes and guidance

In this small step, children explore flexible partitioning of numbers up to 10,000 , understanding that the whole number can be split into parts in many different ways.
Children use numerals, words and expanded form in their partitioning. A key focus should be appreciating that, for example, $6,000+400+20+9=5,000+1,400+20+9$, as this is crucial to understanding addition and subtraction of 4 -digit numbers in future blocks.
The representations used in previous small steps can provide support, arranging place value counters or base 10 to appreciate that the different partitions give the same number. When working in adjacent columns in a place value chart, links should be made to exchanges as this will support learning in later blocks.

## Things to look out for

- Children may believe that 4-digit numbers can only be partitioned one way into thousands, hundreds, tens and ones.
- When identifying a number that has been partitioned in a non-standard way, children may just combine the digits rather than consider their place value, for example $5,000+1,400+20+9=51,429$


## Key questions

- How can you write the number using a part-whole model?
- What different multiples of 1,000 could be the first part? How does this affect the values of the other parts?
- What can you exchange the thousands/hundreds/tens/ones digit for?
- How do you work out the whole, given the parts?


## Possible sentence stems

- $\qquad$ is equal to $\qquad$ thousands, $\qquad$ hundreds,
$\qquad$ tens and $\qquad$ ones or $\qquad$ thousands,
___ hundreds, $\qquad$ tens and $\qquad$ ones.
- $\qquad$ $=$ $\qquad$ $+$ $\qquad$ $+$ $\qquad$ $+$ $\qquad$
or $\qquad$ $+$ $\qquad$ $+$ $\qquad$ $+$ $\qquad$


## National Curriculum links

- Recognise the place value of each digit in a 4-digit number (thousands, hundreds, tens and ones)
- Identify, represent and estimate numbers using different representations


## Flexible partitioning of numbers to 10,000

## Key learning

- Complete the number sentences.

$2,323=2,000+$ $\qquad$ $+$ $\qquad$ $+$
$2,323=$ $\qquad$ $+$ $\qquad$ $+$ $\qquad$ $+$ $\qquad$

How else can 2,323 be partitioned?

- Use the place value chart to complete the number sentences.

| Thousands | Hundreds | Tens | Ones |
| :--- | :---: | :---: | :---: |
| (10) (10) | (10) (10) | (10) (10) (10) | (1) (1) |
|  |  |  |  |
|  |  |  | (1)(1) (1) |

$$
\begin{aligned}
& 2,339=2,000+\ldots+30+9 \\
& 2,339=2,000+300+\ldots+19 \\
& 2,339=1,000+\ldots+30+9
\end{aligned}
$$

- Complete the part-whole models.


What is the same and what is different?

- Here is one way of partitioning 5,426 into two parts.


Find three other ways of partitioning 5,426 into two parts. Compare answers with a partner.

- Complete the number sentences.
- 8,432 $=7,000+$ $\qquad$ $+31$
- 6,729 $=3,000+$ $\qquad$ $+19+$ $\qquad$
- $9,310=$ $\qquad$ $+110+$ $\qquad$
Is there more than one way of completing each sentence?


## Flexible partitioning of numbers to 10,000

## Reasoning and problem solving

Some place value counters are hidden.

The total is six thousand, four hundred and thirty-two.


Which place value counters could be hidden?

Find at least three solutions.

Which is the odd one out?
$3,500 \quad 3$ thousands +50 tens

2 thousands +15 hundreds 35 tens

Explain how you know.

Scott and Esther are each thinking of a number.

- Scott's number has 53 hundreds, 6 tens and 2 ones.
- Esther's number has 5 thousands,

Scott 36 tens and 1 one.

Who is thinking of the greater number?

How do you know?
35 tens $=350$
multiple possible answers, e.g.
1 thousand and 1 hundred

10 hundreds and 10 tens

11 hundreds

Find 1, 10, 100, 1,000 more or less

## Notes and guidance

In Year 3, children found 1, 10 and 100 more or less than a 3-digit number. In this small step, they find 1, 10, 100 and 1,000 more or less than a number with up to four digits.

Using base 10, place value counters and plain counters in a place value chart will support understanding, particularly when multiples of $10 / 100 / 1,000$ are crossed. It is also important to explore examples that result in zero as a placeholder, as this concept needs regular reinforcing.

Draw attention to which place value columns change and which stay the same in each example. This allows children to generalise that, for example, when finding 100 more/less, the ones and tens never change, the hundreds always change and the thousands sometimes change.

## Things to look out for

- Calculations that cross a boundary may cause confusion.
- Children may need support with the use of zero as a placeholder.
- Children may think that when finding, for example, 100 less than a number, only the digit in the hundreds column will ever change.


## Key questions

- How many ones/tens/hundreds/thousands are in $\qquad$ ? How will the number change if you add an extra 1/10/100/1,000?
- Which column changes if you find 1,000 more/less than a number?
- Can finding 1/10/100 more/less change more than one column? When does this happen?
- Do you need to make an exchange?
- How can you find 100 less than 8,012 ? What exchange do you need to make?
- Which columns stay the same/change?


## Possible sentence stems

- There are ___ tens/hundreds/thousands in $\qquad$
- 1 more/less ten than ____ tens is ___ tens.
- $\qquad$ more/less than $\qquad$ is $\qquad$


## National Curriculum links

- Find 1,000 more or less than a given number

Find 1, 10, 100, 1,000 more or less

## Key learning

- Complete the sentences.


The number is $\qquad$
1 less than the number is $\qquad$
10 less than the number is $\qquad$
100 less than the number is $\qquad$
1,000 less than the number is $\qquad$

Complete the sentences.

| Thousands | Hundreds | Tens | Ones |
| :---: | :---: | :---: | :---: |
| 1000 | 1000 | (100) (10) | 1 |
| 1000 |  |  | 1 |
| 1000 |  |  | 1 |

The number is $\qquad$
1 more than the number is $\qquad$
10 more than the number is $\qquad$
100 more than the number is $\qquad$
1,000 more than the number is $\qquad$

- The place value chart shows that 100 more than 4,932 is 5,032

| Thousands | Hundreds | Tens | Ones |
| :---: | :---: | :---: | :---: |
|  |  | (10) (1) (10) | (1) (1) |

Use this method to find the values.

| 100 more |
| :---: |
| than 3,904 | 10 more

than 1,993

1 more than 8,999

- The place value chart shows that 10 less than 3,402 is 3,392

| Thousands | Hundreds | Tens | Ones |
| :---: | :---: | :---: | :---: |
| (20) (10) (10) | (10) 80 |  | (1) (1) |

Use this method to find the values.
100 less than 2,034
10 less than 1,903

## Find 1, 10, 100, 1,000 more or less

## Reasoning and problem solving

Are the statements always true, sometimes true or never true?

$$
\begin{aligned}
& \text { When you find } 100 \text { more or less than } \\
& \text { a number, the tens column changes. }
\end{aligned}
$$

> When you find 10 more or less than a number, the tens column changes.

When you find 1 more or less than a number, the thousands column changes.

Explain your reasoning.

Ron and Dora are thinking of different numbers.

1,000 more than Ron's number is 3,942

Dora's number is 100 more than Ron's number.

What are Ron and Dora's numbers?
never true
always true
sometimes true

Ron: 2,942
Dora: 3,042

Tiny has put some counters on a place value chart.

One counter has fallen off.


List all the possible numbers that Tiny could have started with.

Complete the function machines.


6,043
5,143
5,053
5,044

5,896

- 1,000

1,086

## Notes and guidance

Building on previous learning of number lines to 1,000, children now move on to look at number lines to 10,000

Children label, identify and find missing values on blank or partially completed number lines. Using real-life scales, such as rulers and measuring jugs, can be helpful here.
When looking at partially completed number lines, it is important children become confident in finding the difference between the start and end points and dividing to find the value of each interval. Examples should be used that have a varying number of intervals and unmarked values in different positions.
Children should also be able to work out the value at the midpoint of an interval.

## Things to look out for

- Children may count the number of divisions, rather than the intervals.
- Support may be needed to work out the midpoint of an interval.
- Children may assume the increments on the number line are each worth one unit, focusing solely on the starting number.


## Key questions

- What are the values at the start and end points of the number line?
- What is the difference in value between the start and end points?
- How many intervals are there?
- How can you work out what each interval is worth?
- How can you work out the halfway point of an interval?
- What other numbers can you mark on the number line?
- Why are the start and end values of a number line important?


## Possible sentence stems

- The difference in value between the start and end of the number line is $\qquad$
- There are $\qquad$ intervals. Each interval is worth $\qquad$


## National Curriculum links

- Identify, represent and estimate numbers using different representations
- Order and compare numbers beyond 1,000


## Number line to 10,000

## Key learning

- What numbers are the arrows pointing to?

- Label the number lines.

- Mark the positions of the numbers on the number line.

- Label 5,100 and three other numbers on the number line.


Compare answers with a partner.

- For each number line, estimate the number the arrow is pointing to.



## Reasoning and problem solving



Children should draw an arrow in the correct position on each number line.


Explain the mistake that Tiny has made.

There are 6 divisions, but only 5 intervals.
Tiny needs to divide by 5

What could the start and end numbers be?

multiple possible answers, e.g. 5,000 and 7,000

## Notes and guidance

In previous years, children explored estimating on number lines. In this small step, they estimate on number lines up to 10,000

Children discuss suitable estimates from the information given on the number line and the value of each interval, justifying their choices. Encourage children to identify the midpoint and to mark on additional points, for example one-quarter and three-quarters of the way along, to help them position the numbers.

It may be useful to consider the position of numbers relative to the midpoint of a number line, for example 6,429 is closer to 6,000 than 7,000 and it is less than halfway between the two points. This will be a useful skill later in the block when children look at rounding.

## Things to look out for

- Children may worry that they need to find the exact position or value.
- The scale may be misinterpreted, for example thinking a mark close to 10,000 is 9,999 when 9,000 would be more appropriate.


## Key questions

- What is the midpoint of the number line?
- How does knowing the midpoint help you to place the number on the number line?
- What other numbers could you mark on accurately?
- Which division is the arrow close to? Is the number greater than or less than this value?
- How would splitting the line into more intervals help?
- How accurate do you think your estimate is?


## Possible sentence stems

- The difference in value between the start and end of the number line is $\qquad$
- The midpoint of the number line is $\qquad$
- $\qquad$ is closer to $\qquad$ than $\qquad$


## National Curriculum links

- Identify, represent and estimate numbers using different representations
- Order and compare numbers beyond 1,000


## Estimate on a number line to 10,000

## Key learning

- Mark the midpoint of each number line.

What number does each midpoint represent?


- Estimate the numbers the arrows are pointing to.

- Alex and Dexter are marking 8,000 on the number line.


Whose method did you find easier?
Which method do you think is more accurate?

- Draw arrows to show the approximate positions of the numbers on the number line.


Compare methods with a partner.

## Estimate on a number line to 10,000

## Reasoning and problem solving

Mo and Teddy are estimating the number that the arrow is pointing to.


Who do you agree with?
Explain your answer.

Teddy's estimate is more realistic. The midpoint is 5,000 10 would be much closer to zero.

Miss Rose has spilt some paint on the number line.


Estimate three numbers that could appear under the paint.
Explain your answers.
numbers between 3,000 and 7,500


- $C$ is greater than $A$.
- C is less than half of B.

Give three possible values for $C$.
e.g. $A=1,500 \quad B=9,000 \quad C=$ between 1,500 and 4,500

## Notes and guidance

This small step focuses on comparing numbers up to 10,000 using language such as greater/smaller than, less/more than. Once they are confident with the language used for comparisons, children progress to using the inequality symbols, $<,>$ and $=$, which they have encountered in previous years.

Representations such as base 10, place value counters and charts, and number lines support children's understanding of place value, allowing them to compare numbers visually before moving on to more abstract forms.

Demonstrate to children that when comparing numbers, they need to start with the greatest place value. If the digit in the greatest place value is the same, they need to look at columns to the right until they find different digits.

## Things to look out for

- When comparing numbers, children may compare the smallest place value first.
- Children may interpret the inequality symbols incorrectly, confusing < and >
- Children may be confused by numbers with a different number of digits or numbers that contain placeholders.


## Key questions

- What is the value of the first digit in $\qquad$ ?
- What is the value of the $\qquad$ digit in $\qquad$ ?
- How many thousands/hundreds/tens/ones are there?
- Which column do you start comparing from?
- Which digit in each number has the greatest value? What is the value of these digits?
- When comparing two numbers, if the first digits are equal in value, what do you look at next?
- Which is the greater number? How do you know?


## Possible sentence stems

- If the digits in the $\qquad$ column are the same, I need to look in the $\qquad$ column.
- $\qquad$ is greater than $\qquad$ because ...
- $\qquad$ is less than $\qquad$ because ...


## National Curriculum links

- Order and compare numbers beyond 1,000


## Compare numbers to 10,000

## Key learning

- Which is the greater number? How do you know?


Complete the sentences.
$\qquad$ is less than $\qquad$
$\qquad$ is greater than $\qquad$

- Write <, > or = to compare the numbers.

- A laptop costs $£ 2,453$

A TV costs $£ 2,435$
Which item is more expensive?


- Complete the statements.

| Th | H | T | O |
| :---: | :---: | :---: | :---: |
| 8 | 0 | 3 | 4 |
| 8 | 0 | 2 | 9 |

8,034 is $\qquad$ than 8,029
8,029
 8,034

- Write <, > or = to compare the numbers.

 1,032
 1,897

4,238


 865

1,920


## Compare numbers to 10,000

## Reasoning and problem solving



## Notes and guidance

In this small step, children order a set of numbers up to 10,000 Children order numbers from the smallest to the greatest and the greatest to the smallest. They also use language such as "ascending" and "descending" when putting the numbers in order. Children are given examples where the same digit is used in the thousands or the hundreds column so that they need to look at the other digits to determine the value. They also include zero in different places to check understanding of placeholders.

Base 10 and place value counters are used to represent numbers to help children make comparisons. Making links with numbers in real-life situations, such as prices and measurements, is also useful.

## Things to look out for

- Children may just look at the digits and not consider the place value.
- Children may need to be reminded of the meanings of the words "ascending" and "descending".
- Children may need to be reminded about inequality symbols and their meanings.


## Key questions

- Which digit in each number has the greatest value? What are the values of these digits?
- When comparing two numbers with the same number of digits, if the first digits are equal in value, what do you look at next?
- What is the difference between ascending and descending order?
- What is different about comparing numbers with the same number of digits and comparing numbers with different numbers of digits?


## Possible sentence stems

- $\qquad$ is greater than $\qquad$ , so $\qquad$ thousand is greater than ___ thousand.
- $\qquad$ is less than $\qquad$ , so $\qquad$ thousand is less than
$\qquad$ thousand.


## National Curriculum links

- Order and compare numbers beyond 1,000


## Order numbers to 10,000

## Key learning

- Nijah, Dani and Brett are making numbers with base 10


Who has made the greatest number?
Who has made the smallest number?
How do you know?

- Tom makes four numbers using place value counters.


| Th | $H$ | T | O |
| :---: | :---: | :---: | :---: |
| (100) |  |  |  |



Write Tom's numbers in order, from the smallest to the greatest.

- Here are four digit cards.


Arrange them to make five different 4-digit numbers. Put your numbers in ascending order.

- Put four counters in the place value chart to make six different numbers.

| Thousands | Hundreds | Tens | Ones |
| :--- | :--- | :--- | :--- |
|  |  |  |  |
|  |  |  |  |

Write your numbers in descending order.

- Write the amounts in order. Start with the smallest amount.


Write the measurements in order. Start with the greatest measurement.


## Order numbers to 10,000

## Reasoning and problem solving



## Roman numerals

## Notes and guidance

Children build on their knowledge of Roman numerals from 1 to 12 on a clock face, and learn that L represents 50 and C represents 100

Children explore the similarities and differences between the Roman number system and our number system, understanding that the Roman system does not have a zero and does not use placeholders. They are already familiar with the idea that, for example, 4 is written as IV rather than IIII, and they apply the same concept to write 40 as XL and 90 as XC.

Roman numerals can be revisited later in this block (for example, rounding XXV to the nearest 10) or within the addition and subtraction block.

## Things to look out for

- Children may mix up which letter stands for which number.
- Children may add the individual values together instead of interpreting the values based on their position, for example interpreting XC as 110 instead of 90
- It is more difficult to convert numbers that require large strings of Roman numerals.
- Children may think that numbers like 99 can be written as IC instead of XCIX.


## Key questions

- What patterns can you see in the Roman number system?
- What rules do you use when converting numbers to Roman numerals?
- What letters are used in the Roman number system? What does each letter represent?
- How do you know what order to write the letters in when using Roman numerals?
- What is the same and what is different about representing the number twenty-nine in the Roman number system and our number system?


## Possible sentence stems

- The letter $\qquad$ represents the number $\qquad$
- I know $\qquad$ is greater than $\qquad$ because $\qquad$


## National Curriculum links

- Read Roman numerals to 100 (I to C) and know that over time, the numeral system changed to include the concept of zero and place value


## Roman numerals

## Key learning

- Write each number in Roman numerals.


64


78


85

- Choose the correct answer to each calculation.

| - L + L | LL | X |
| :---: | :---: | :---: |
| - $\mathrm{C}-\mathrm{X}$ | CX | XC |
| - IX + XI | XX | XXII |

- Complete the function machines.

- Each diagram should show a number in numerals, words and Roman numerals.
Complete the diagrams.

- Write $<$, > or = to complete the statements.





$L x$



## Roman numerals

## Reasoning and problem solving

Is the statement true or false?

$$
\begin{gathered}
\text { XX + II = XXII, } \\
\text { so XXII + XXII = XXIIXXII }
\end{gathered}
$$

Explain your answer.

Work out the calculation, giving your answer in Roman numerals.
XIV + XXXVI

Make up some other calculations using Roman numerals that have the same answer.


L
multiple possible answers, e.g.
$\mathrm{C} \div \mathrm{II}$
$\mathrm{L} \div \mathrm{I}$
$x \times v$
$X X V \times I I$

In the 10 times-table, all multiples of 10 end in a zero. This means that in Roman numerals multiples
of 10 end in X .


Is Tiny's statement always, sometimes or never true?

Give examples to support your answer.

Which of these Roman numerals is never written to the left of $X$ ?

sometimes true, e.g. $20=$ XX, 80 = LXXX
sometimes false, e.g. $50=\mathrm{L}$ and $100=\mathrm{C}$

V

## Notes and guidance

In this small step, children are introduced to rounding for the first time, starting with rounding to the nearest 10

Children begin by focusing on rounding 2-digit numbers, as it is clearer what the previous and next multiples of 10 are.
When building on this and starting to round 3-digit numbers, it is important to include examples that have zero as a placeholder in the tens column, for example 304, as children can often think that 300 is not a multiple of 10 because it is a multiple of 100

Number lines can be used not only to identify the previous and next multiple of 10, but also which multiple of 10 a number is closer to. Children should understand the convention that when the ones digit is 5 , they round to the next multiple of 10

Avoid using language such as "round up" and "round down", as this can create misconceptions.

## Things to look out for

- Children may look at the wrong column when deciding which way to round, and use the tens column instead of the ones column.
- Children may think that, for example, 52 "rounds down" and give the result as 42 or 40


## Key questions

- What is the multiple of 10 after $\qquad$ ?
- What is the multiple of 10 before $\qquad$ ?
- Which multiple of 10 is $\qquad$ closer to? How do you know?

Which numbers rounded to the nearest 10 result in zero?

- Which place value column do you need to look at to decide which multiple to round to?
- What numbers when rounded to the nearest 10 give the result 50/500?


## Possible sentence stems

- The two multiples of 10 the number lies between are $\qquad$ and $\qquad$ -
- $\qquad$ is closer to $\qquad$ than $\qquad$
- $\qquad$ rounded to the nearest 10 is $\qquad$


## National Curriculum links

- Round any number to the nearest 10,100 or 1,000


## Round to the nearest 10

## Key learning

- Use the number lines to help you complete the sentences.


13 is closer to $\qquad$ than $\qquad$
13 rounded to the nearest 10 is $\qquad$


78 is closer to $\qquad$ than $\qquad$ _


378 is closer to $\qquad$ than $\qquad$ -
378 rounded to the nearest 10 is $\qquad$
375 rounded to the nearest 10 is $\qquad$

- Use the number line to help you complete the sentences.


143 rounded to the nearest 10 is $\qquad$
146 rounded to the nearest 10 is $\qquad$
145 rounded to the nearest 10 is $\qquad$
150 rounded to the nearest 10 is $\qquad$

- Round each number to the nearest 10
- Which numbers round to 760 to the nearest 10 ?

| 761 | 765 | 760 | 763 | 755 |
| :--- | :--- | :--- | :--- | :--- |

- Round each number to the nearest 10



## Round to the nearest 10

## Reasoning and problem solving



When rounded to the nearest 10,
there are 350 children in
a running club.
How many children could there be?

## Jack



345, 346, 347, 348,
349, 350, 351, 352,
353 or 354

If the ones digit is a 5 , the number rounds to the next multiple of 10

445 rounds to 450

## Notes and guidance

Building on the previous step, children now begin to round numbers to the nearest 100

Children begin by focusing on rounding 3-digit numbers, as it is clearer what the previous and next multiples of 100 are. It is important to discuss what is the same and what is different when rounding numbers to 10 and 100. By doing this, children can begin to understand that when asked to round to a given amount, they need to look at the next place value column to the right.

It is helpful to use examples that are less than 50 , so children see that these round to the previous multiple of 100 , which is zero.
As in the previous step, avoid using language such as "round up" and "round down", as this can create misconceptions.

## Things to look out for

- Children may look at the wrong column to decide which way to round and use the hundreds column instead of the tens column.
- Children may focus on rules about "up" and "down" instead of looking at multiples of 100, for example rounding 432 to 402 or 332


## Key questions

- What is the multiple of 100 after $\qquad$ ?
- What is the multiple of 100 before $\qquad$ ?
- Which multiple of 100 is $\qquad$ closer to? How do you know?
- Which numbers rounded to the nearest 100 result in zero?
- Which place value column do you need to look at to decide which multiple to round to?
- What is the same and what is different about rounding to the nearest 10 and rounding to the nearest 100?


## Possible sentence stems

- The two multiples of 100 the number lies between are $\qquad$ and $\qquad$ -
- $\qquad$ is closer to $\qquad$ than $\qquad$
- $\qquad$ rounded to the nearest 100 is $\qquad$


## National Curriculum links

- Round any number to the nearest 10,100 or 1,000


## Round to the nearest 100

## Key learning

- Which multiples of 100 do the numbers lie between?


Use the number line to help you complete the sentences.
340 is closer to $\qquad$ than $\qquad$ -

340 rounded to the nearest 100 is $\qquad$

- Complete the number line and the sentences.


1,610 is closer to $\qquad$ than $\qquad$
1,610 rounded to the nearest 100 is $\qquad$
1,681 is closer to $\qquad$ than $\qquad$
1,681 rounded to the nearest 100 is $\qquad$
1,650 rounded to the nearest 100 is $\qquad$

- Round each number to the nearest 100
- Round each number to the nearest 100


LXXI


## Round to the nearest 100

## Reasoning and problem solving



To the nearest 100, there are 600 people at a football match.

What is the smallest number of people that could be at the football match?
What is the greatest number of people that could be at the football match?
How would your answers change if the number of people at the football match was 600 when rounded to the nearest 10 ?

To the nearest 100 , there are 4,600 people at a concert.
The sum of the digits in the number is 15

How many people could there be?

Tommy is thinking of a number.


What number could Tommy be thinking of?
How many answers can you find?

4,551, 4,560, 4,605,
4,614, 4,623, 4,632,
4,641


> 4,450 to 4,494
> 4,505 to 4,549

## Round to the nearest 1,000

## Notes and guidance

Building on the previous small steps, children round numbers to the nearest 1,000

Children begin by discussing which multiple of 1,000 a number is closest to. They can then identify that if the digit in the hundreds column is between zero and 4 , they round to the previous multiple of 1,000 , but if the digit in the hundreds column is 5 or above, they round to the next multiple of 1,000
Children make links with rounding numbers to the nearest 10 or 100, all of which are explored in the next step.

It is helpful to use examples that are less than 500 , so children see that these round to the previous multiple of 1,000 , which is zero.

As in the previous steps, avoid language such as "round up" and "round down", as this can create misconceptions.

## Things to look out for

- Children may look at the wrong column to decide which way to round and use the thousands column instead of the hundreds column.
- Children may focus on rules about "up" and "down" instead of looking at multiples of 1,000 , for example rounding 6,432 to 5,432


## Key questions

- What is the multiple of 1,000 after $\qquad$ ?
- What is the multiple of 1,000 before $\qquad$ ?
- Which multiple of 1,000 is $\qquad$ closer to? How do you know?
- Which numbers rounded to the nearest 1,000 result in zero?
- Which place value column do you need to look at to decide which multiple to round to?
- What is the same and what is different about rounding to the nearest 10,100 and 1,000 ?


## Possible sentence stems

- The two multiples of 1,000 the number lies between are
$\qquad$ and $\qquad$
- $\qquad$ is closer to $\qquad$ than $\qquad$
- $\qquad$ rounded to the nearest 1,000 is $\qquad$


## National Curriculum links

- Round any number to the nearest 10,100 or 1,000


## Round to the nearest 1,000

## Key learning

- Use the number lines to help you complete the sentences.
4,300 rounded to the nearest 1,000 is $\qquad$


7,650 is closer to $\qquad$ than $\qquad$
7,650 rounded to the nearest 1,000 is $\qquad$

- Complete the number line.


Draw an arrow to show 8,550 on the number line.
8,550 rounded to the nearest 1,000 is $\qquad$

## Round to the nearest 1,000

## Reasoning and problem solving

Each of the numbers round to 4,000
to the nearest 1,000
What could the missing digits be?

| $4, \ldots 28$ |
| :--- |
| $4,2 \ldots 8$ |



Do you agree with Tiny?
Explain your answer.


Rosie makes a 4-digit number using the digit cards.


What number could Rosie have made? Is there more than one possibility?

5,649, 5,694, 5,946,
5,964, 6,459, 6,495

## Notes and guidance

In this small step, children round to the nearest 10, 100 or 1,000, choosing the appropriate columns to look at.

Discuss with children what is the same and what is different when rounding numbers to the nearest 10,100 or 1,000 .
Ensure children understand that when asked to round to a given amount, they need to look at the place value column to the right of that of the required accuracy to decide whether to round to the previous or next multiple. It is worth discussing with children when each degree of accuracy is more appropriate.
As with the previous steps, avoid language such as "round up" and "round down", as this can create misconceptions.

## Things to look out for

- When rounding numbers to different degrees of accuracy, children may look at the wrong column(s).
- Children may not realise that the answer can be the same when a number is rounded to different degrees of accuracy.
- When rounding the same number to different degrees of accuracy, children may not always use the starting number but, for example, round it to the nearest 10, then round this value to the nearest 100 and so on.


## Key questions

- What is the multiple of $10 / 100 / 1,000$ after $\qquad$ ?
- What is the multiple of $10 / 100 / 1,000$ before $\qquad$ ?
- Which multiple of $10 / 100 / 1,000$ is $\qquad$ closer to? How do you know?
- Which numbers rounded to the nearest 10/100/1,000 result in zero?
- Which place value column do you need to look at to decide which multiple to round to?
- What is the same and what is different about rounding to the nearest 10,100 and 1,000 ?


## Possible sentence stems

- The two multiples of 10/100/1,000 the number lies between are $\qquad$ and $\qquad$
- $\qquad$ is closer to $\qquad$ than $\qquad$
- $\qquad$ rounded to the nearest $10 / 100 / 1,000$ is $\qquad$


## National Curriculum links

- Round any number to the nearest 10,100 or 1,000


## Round to the nearest 10, 100 or 1,000

## Key learning

- Draw an arrow to mark 376 on each number line.

Complete the sentences.


376 rounded to the nearest 10 is $\qquad$


376 rounded to the nearest 100 is $\qquad$


376 rounded to the nearest 1,000 is $\qquad$

- Here is a number.


Round the number to the nearest 10,100 and 1,000

- Complete the table.

| Number | 7,126 | 4,996 | 2,006 | 499 |
| :---: | :--- | :--- | :--- | :--- |
| Rounded to the <br> nearest 10 |  |  |  |  |
| Rounded to the <br> nearest 100 |  |  |  |  |
| Rounded to the <br> nearest 1,000 |  |  |  |  |

- A baker uses $4,285 \mathrm{~g}$ of flour.

Round the mass of flour to the nearest 100 g .
Round the mass of flour to the nearest 10 g .
Round the mass of flour to the nearest kilogram.
Which do you think is the most appropriate way of rounding the number?

- A school fete raises $£ 2,166$

Round this amount to the nearest $£ 10$, nearest $£ 100$ and nearest $£ 1,000$
Which do you think is the most appropriate way of rounding the number?

## Reasoning and problem solving



## Autumn Block 2

## Addition and subtraction

Step 1 Add and subtract $1 \mathrm{~s}, 10 \mathrm{~s}, 100 \mathrm{~s}$ and $1,000 \mathrm{~s}$

| Step 2 | Add up to two 4-digit numbers - no exchange |
| :--- | :--- |
| Step 3 | Add two 4-digit numbers - one exchange |
| Step 4 | Add two 4-digit numbers - more than one exchange |
| Step 5 | Subtract two 4-digit numbers - no exchange |
| Step 6 | Subtract two 4-digit numbers - one exchange |
|  |  |
| Step 7 | Subtract two 4-digit numbers - more than one exchange |

## Small steps

Step 9 Estimate answers

Step 10 Checking strategies

## Notes and guidance

In Year 3, children explored adding and subtracting 1s, 10 s and 100 s to/from any 3 -digit number, including using a mental strategy when crossing a multiple of 10 or 100

In this small step, children recap this learning and extend their understanding to dealing with 4-digit numbers and adding and subtracting multiples of 1,000 . The focus is on mental rather than written strategies, which are covered later in the block.
It is important to explore the effect of either adding or subtracting a multiple of $1,10,100$ or 1,000 by discussing which columns always, sometimes and never change. For example, when adding a multiple of 100, the ones and tens never change, the hundreds always change and the thousands sometimes change, depending on the need to make an exchange.

## Things to look out for

- Children may identify the incorrect place value column, particularly if they are using plain counters in a place value chart, for example 3,469-300 $=469$ or 3,439
- Confusion may arise with zero as a placeholder.
- Children may find crossing the next or previous multiple challenging.


## Key questions

- If you know $2+4=6$, what else do you know?
- How will you partition $\qquad$ ? Why?
- Will the value in the ones/tens/hundreds/thousands column increase or decrease? By how much?
- Which place value columns have changed/stayed the same? Why?
- What is the inverse of subtracting 300 ?


## Possible sentence stems

- The next/previous multiple of $10 / 100 / 1,000$ is $\qquad$
- I can partition $\qquad$ into $\qquad$ and $\qquad$ because ...
- The value of the $\qquad$ column will increase/decrease by $\qquad$


## National Curriculum links

- Add and subtract numbers with up to four digits using the formal written methods of columnar addition and subtraction where appropriate
- Solve addition and subtraction two-step problems in contexts, deciding which operations and methods to use and why


## Add and subtract $1 \mathrm{~s}, 10 \mathrm{~s}, 100$ s and $1,000 \mathrm{~s}$

## Key learning

- Complete the part-whole models and number sentences.


What do you notice?

- Use a place value chart to help you complete the number sentences.

$$
\begin{aligned}
& 1,364+3= \\
& 1,364+30= \\
& 1,364+300=
\end{aligned}
$$

$$
1,364-1=
$$

$\qquad$

- $1,364-60=$ $\qquad$
- $1,364-200=$ $\qquad$
- $1,364+6,000=$ $\qquad$ - $1,364-1,000=$ $\qquad$

What do you notice? What stays the same and what changes?

- Amir and Whitney are using number lines to add and subtract.


Use this method to work out the calculations.
$2,418+6$
$2,418+800$
$2,418+90$
$2,418-30$
$2,418-9$
$2,418-700$

- There are 1,286 patients and doctors in a hospital. 300 patients leave after being treated.
Another 90 patients arrive.
7 doctors leave.
How many patients and doctors are in the hospital now?


## Add and subtract $1 \mathrm{~s}, 10$ s, 100 s and 1,000 s

## Reasoning and problem solving



Rosie is finding the missing number in $\qquad$ $-300=2,895$


What mistake has Rosie made?
Work out the missing number.

Ron is partially correct. However, the thousands may also change, e.g. $1,983+30=2,013$

Rosie has subtracted 300 from the answer rather than using the inverse.

3,195

Here is a number on a place value chart.



What number could Tiny have now?
multiple possible answers, e.g.
2,892, 3,792,
3,882, 3,891
1,092

## Add up to two 4-digit numbers - no exchange

## Notes and guidance

In Year 3, children used the formal written method to add two 2- or 3-digit numbers, with up to two exchanges. In this block, that learning is extended to include 4-digit numbers. In this small step, they add 3 - or 4-digit numbers with no exchanges, using concrete resources as well as the formal written method.

The numbers being added together may have a different number of digits, so children need to take care to line up the digits correctly. Even though there will be no exchanging, the children should be encouraged to begin adding from the ones column. When working within each column, ask, "Do you have enough ones/tens/hundreds to make an exchange?" This will prepare them for future small steps where exchanging will be necessary.

## Things to look out for

- Children may not line up the digits in the place value columns correctly.
- Children may assume they should start adding from left to right. Be careful as this may appear to be a good strategy given there are no exchanges required in this small step.
- Children may not use zero as a placeholder when there are no hundreds, tens or ones.


## Key questions

- How can you represent the question using base 10?
- How can you put these numbers into a place value chart?
- Does it matter which columns you add together first?
- Do you have enough ones/tens/hundreds to make an exchange?
- What do you write in the tens column if there are no tens?


## Possible sentence stems

- $\qquad$ ones added to $\qquad$ ones is equal to $\qquad$ ones.
$\bullet$ $\qquad$ added to $\qquad$ is equal to $\qquad$
- I have $\qquad$ ones, so I do/do not need to make an exchange.


## National Curriculum links

- Add and subtract numbers with up to four digits using the formal written methods of columnar addition and subtraction where appropriate
- Solve addition and subtraction two-step problems in contexts, deciding which operations and methods to use and why


## Add up to two 4-digit numbers - no exchange

## Key learning

- Use counters and a place value chart to work out 3,256 + 2,532

- Complete the additions.


- Fill in the missing numbers.

- Work out the missing numbers.

- Tommy walks 3,420 m.

Eva walks 356 m.
How far do they walk altogether?

## Add up to two 4-digit numbers - no exchange

## Reasoning and problem solving

Tiny works out $1,234+345$


## Add two 4-digit numbers - one exchange

## Notes and guidance

Building on the previous small step, children now add two 4-digit numbers with one exchange in any column. In Year 3, they explored 3-digit addition with up to two exchanges, so they should be familiar with the process.
The numbers can be made using concrete manipulatives such as place value counters in a place value chart, alongside the formal written method. When discussing where to start an addition, it is important to use language such as begin from the "smallest value column" rather than the "ones column" to avoid any misconceptions when decimals are introduced later in the year.
After each column is added, ask, "Do you have enough ones/ tens/hundreds to make an exchange?" This question will be an important one in this small step, as the children do not know which column will be the one where an exchange is needed.

## Things to look out for

- Children may not line up the digits in the place value columns correctly.
- Children may not add up from the smallest value column, and so will not be able to exchange correctly.
- Children may not use zero as a placeholder when there are no hundreds, tens or ones.


## Key questions

- How many thousands/hundreds/tens/ones are there altogether?
- What is $\qquad$ more than $\qquad$ ?
- Does it matter which columns you add together first?
- Do you have enough ones/tens/hundreds to make an exchange?
- When exchanging 10 hundreds, where do you put the thousand?


## Possible sentence stems

- $\qquad$ ones added to $\qquad$ ones is equal to $\qquad$ ones.
- $\qquad$ added to $\qquad$ is equal to $\qquad$
- I have $\qquad$ hundreds, so I do/do not need to make an exchange.
- I can exchange 10 $\qquad$ for 1 $\qquad$


## National Curriculum links

- Add and subtract numbers with up to four digits using the formal written methods of columnar addition and subtraction where appropriate
- Solve addition and subtraction two-step problems in contexts, deciding which operations and methods to use and why


## Add two 4-digit numbers - one exchange

## Key learning

- Kim uses counters to find the total of 3,356 and 2,435


Use Kim's method to work out the additions.

```
3,356 + 2,437
```

$3,356+2,473$
$3,356+2,743$

- Complete the bar models.


| 1,185 | 405 |
| :--- | :--- |
|  |  |

- Find the sum of 6,825 and 1,344
- Brett has 3,436 marbles.

Huan has 1,293 more marbles than Brett.
How many marbles does Huan have?
Brett


Huan


- Esther has 1,214 stickers.

Sam has 1,123 more stickers than Esther.
How many stickers do they have altogether?
Esther

Sam


- Eva has 1,434 pennies.

Tom has 1,158 more pennies than Eva.
How many pennies does Tom have?

## Add two 4-digit numbers - one exchange

## Reasoning and problem solving

Tiny completes this addition.

|  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Th | $\mathbf{H}$ | $\mathbf{T}$ | $\mathbf{O}$ |  |
|  |  | 4 | 0 | 8 | 6 |  |
|  | + | 1 | 5 | 3 | 2 |  |
|  |  | 5 | 5 | 1 | 9 |  |
|  |  |  |  | 1 |  |  |



Dexter adds a 4-digit number to a 2-digit number.

multiple possible
answers, e.g.
$9,025+65$
$9,040+50$
$8,991+99$

## Add two 4-digit numbers - more than one exchange

## Notes and guidance

Building on the previous small step, children now add two 4-digit numbers with more than one exchange.

The numbers are made using place value counters in a place value chart alongside the formal written method. The addition begins from the smallest value column. After each column is added, ask, "Do you have enough ones/tens/hundreds to make an exchange?" This question is important at every stage as there will be more than one exchange to make. With more than one exchange, it is important to model the correct place to write the number exchanged and to add it to the next column.

## Things to look out for

- Children may not line up the digits in the place value columns correctly, especially the digits created by exchanging.
- Children may forget to add from the smallest value column first.
- Children may not realise that two digits that look as though they will not total enough to make an exchange could do so once an exchange has happened, for example $5+4$ plus an extra 1 exchanged from the previous column.


## Key questions

- How many ones/tens/hundreds/thousands are there in total?
- What is $\qquad$ more than $\qquad$ ?
- Does it matter which columns you add together first?
- Do you have enough ones/tens/hundreds to make an exchange?
- How can you make an exchange in more than one column in the same addition?


## Possible sentence stems

- ___ ones added to ___ ones is equal to ___ ones.
- $\qquad$ plus $\qquad$ plus the 1 that I exchanged from the last column is equal to $\qquad$
- I have $\qquad$ hundreds/tens/ones, so I do/do not need to make an exchange.


## National Curriculum links

- Add and subtract numbers with up to four digits using the formal written methods of columnar addition and subtraction where appropriate
- Solve addition and subtraction two-step problems in contexts, deciding which operations and methods to use and why


## Add two 4-digit numbers - more than one exchange

## Key learning

- Nijah uses place value counters to help her work out $4,673+1,518$


Use Nijah's method to work out the additions.


- Complete the additions.

$$
4,507+1,648
$$

$$
4,507+674
$$

- Jack uses place value counters to work out 1,945 + 1,257


Use Jack's method to work out the additions.

$$
\begin{array}{l|l|l|l}
4,893+1,758 & 3,546+1,794 & 2,305+1,896
\end{array}
$$

- White Rose FC are playing a football match against Red Rose Rovers.

2,438 fans come to watch White Rose FC.
1,765 fans come to watch Red Rose Rovers.
How many fans come to watch the match altogether?

## Add two 4-digit numbers - more than one exchange

## Reasoning and problem solving

Alex is working out this addition.


Is Alex correct?
Explain how you know.

Teddy works out 3,218+1,354


How do you know that Teddy's answer cannot be correct?

Rosie and Mo each have some points on a computer game.
Mo has 599 fewer points than Rosie.
Mo has 4,278 points.
How many points do they have altogether?

When adding two numbers together, the greatest digit that can be carried over is 1

Subtract two 4-digit numbers - no exchange

## Notes and guidance

In Year 3, children used the formal written method to subtract two 2- or 3-digit numbers with up to two exchanges. In this block, that learning is extended to include 4-digit numbers. In this small step, children subtract up to a 4-digit number from a 4-digit number with no exchanges, using concrete resources as well as the formal written method.
Even though there is no exchanging, children should subtract from the smallest value column first. Before subtracting each column, ask, "Do you have enough ones/tens/hundreds to subtract $\qquad$ ?" If not, an exchange is needed.
Encouraging children to subtract from the "smallest value column" first, rather than referring to it as the "ones column", will avoid a misconception when decimals are introduced later in the year.

## Things to look out for

- When using concrete resources, children may make both numbers, then remove the second one, leaving the first number unchanged.
- Children may not line up the digits in the place value columns correctly, especially when the numbers have different numbers of digits.


## Key questions

- How can you show this question using place value counters?
- What is $\qquad$ less than $\qquad$ ?
- Does it matter which column you subtract first?
- Do you need to make an exchange?
- Do you have enough ones/tens/hundreds to subtract $\qquad$ ?


## Possible sentence stems

- ones/tens/hundreds subtract $\qquad$ ones/tens/
hundreds is equal to $\qquad$
I can/cannot subtract $\qquad$ ones/tens/hundreds from
$\qquad$ ones/tens/hundreds, so I do/do not need to make an exchange.


## National Curriculum links

- Add and subtract numbers with up to four digits using the formal written methods of columnar addition and subtraction where appropriate
- Solve addition and subtraction two-step problems in contexts, deciding which operations and methods to use and why


## Subtract two 4-digit numbers - no exchange

## Key learning

- Dora uses place value counters to work out 3,454-1,224


Use Dora's method to work out the subtractions.


- Find the missing numbers.

- Use bar models to help you answer each question.

There are 3,597 boys and girls in a school. 2,182 are boys.
How many girls are there?

Car A travels 7,653 miles per year.
Car B travels 5,612 miles per year. How much further does car A travel than car B per year?

- The mass of a bag of sand is $3,576 \mathrm{~g}$. $1,250 \mathrm{~g}$ of sand is poured from the bag. What is the mass of the bag of sand now?
- Whitney and Amir are at the fair. At each stall, they can win tickets.


How many tickets did Amir win?

## Subtract two 4-digit numbers - no exchange

## Reasoning and problem solving

Tiny is working out 3,426-1,213 using place value counters.
Tiny keeps getting 3,426 as the answer.


Explain Tiny's mistake.
Work out the correct answer.

Fill in the missing digits.


Compare answers with a partner.
Can you find any more?

The mass of a box is $2,479 \mathrm{~g}$. A teddy bear is $1,305 \mathrm{~g}$ lighter than the box.

What is the total mass of the teddy bear and the box?
for example:
$9,999-3,685=6,314$
$9,999-1,680=8,319$
$3,653 \mathrm{~g}$

Subtract two 4-digit numbers - one exchange

## Notes and guidance

Building on the previous small step, children subtract up to 4-digit numbers, with one exchange. In Year 3, children subtracted 2 - and 3-digit numbers with up to two exchanges.

It is important that children complete the formal written method alongside any concrete manipulatives to support understanding.

Before subtracting each column, ask, "Do you have enough ones/tens/hundreds to subtract $\qquad$ ?" If not, then an exchange is needed.

For this small step, the exchange could take place from the tens, hundreds or thousands, but there is only one exchange per calculation.

## Things to look out for

- Children may not line up the digits in the place value columns correctly, especially when the numbers have different numbers of digits.
- Children may find the difference between the two digits in a column instead of subtracting the second digit from the first in order to avoid an exchange, for example 1 - 3 becomes 3-1


## Key questions

- What is ___ less than ___
- Does it matter which column you subtract first?
- Do you need to make an exchange?
- How can you subtract two numbers if one of them has fewer digits than the other?


## Possible sentence stems

- $\qquad$ ones/tens/hundreds subtract $\qquad$ ones/tens/ hundreds is equal to $\qquad$
- I can/cannot subtract $\qquad$ ones/tens/hundreds from $\qquad$ ones/tens/hundreds, so I do/do not need to make an exchange.


## National Curriculum links

- Add and subtract numbers with up to four digits using the formal written methods of columnar addition and subtraction where appropriate
- Solve addition and subtraction two-step problems in contexts, deciding which operations and methods to use and why


## Subtract two 4-digit numbers - one exchange

## Key learning

- Rosie uses base 10 to work out 3,416-1,223

| Thousands | Hundreds | Tens | Ones |
| :---: | :---: | :---: | :---: |
|  |  |  | $\begin{aligned} & \square \\ & \square \square \\ & \square \end{aligned}$ |


|  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Th | $\mathbf{H}$ | $\mathbf{T}$ | $\mathbf{O}$ |  |
|  |  | 3 | $3 / 4$ | ${ }^{3} 1$ | 6 |  |
|  | - | 1 | 2 | 2 | 3 |  |
|  |  | 2 | 1 | 9 | 3 |  |
|  |  |  |  |  |  |  |

Use Rosie's method to help you work out the subtractions.

$$
\begin{array}{l|l|l|l}
4,256-1,139 & 3,758-1,825 & 2,547-1,452
\end{array}
$$

What is the same and what is different about these subtractions?

- Find the missing numbers.

|  | 2,174 |
| ---: | :---: |
| 3,567 |  |

- Ron uses place value counters to work out 2,343-151


Use place value counters to help you work out the subtractions.

$$
5,383-291
$$

$$
3,157-523
$$

$$
9,458-86
$$

- Use bar models to help you complete the questions.

> Mrs Trent has $£ 3,544$
> She spends $£ 1,225$

How much money does she have left?

## Mrs Khan has £1,745

She has $£ 1,239$ more than Mr Khan.
How much money does Mr Khan have?

## Subtract two 4-digit numbers - one exchange

## Reasoning and problem solving

1,235 people go on a school trip.
There are 1,179 children and 27 teachers.

The rest are parents.
How many parents are there?
Explain your method to a partner.

Find the missing numbers.

$$
-1,345=4 \_6
$$

What is the greatest number that could go in the first space?
What is the smallest?
How many possible answers could you have?

What is the pattern between the numbers?
What method did you use?

29 parents

1,841 (and 9)

1,751 (and 0)

10 possible answers

For each answer, both numbers go up by 10

The subtraction has exactly one exchange.


What could the missing numbers be if the exchange is in the tens column?

What if the exchange was in another column?

Talk about it with a partner.
various possible answers, e.g.
2,351 and 3,281
various possible answers, e.g.

3,810 and 1,822

Subtract two 4-digit numbers - more than one exchange

## Notes and guidance

In this small step, children subtract up to 4-digit numbers with more than one exchange, using the written method of column subtraction.

Children perform subtractions involving two separate exchanges (for example, from the thousands and from the tens) as well as those with two-part exchanges (for example, from the thousands down to the tens if there are no hundreds in the first number). To support understanding, continue solving these subtractions alongside the concrete resources of base 10 and place value counters.

When completing the written method, it is vital that children are careful with where they put the digits, especially those that have been exchanged. Two-part exchanges can be confusing for children if they are unsure what each digit represents or where to put it.

## Things to look out for

- Children may not line up the digits in the place value columns correctly.
- When exchanging a number, children may put the 1 in the incorrect place.
- When exchanging over two columns, children may exchange directly from, for example, hundreds down to ones and miss out the exchange to tens.


## Key questions

- Does it matter which column you subtract first?
- Do you need to make an exchange?
- How can you subtract two numbers if one of them has fewer digits than the other?
- If you cannot exchange from the tens/hundreds, what do you need to do?
- Which column can you exchange from?


## Possible sentence stems

- $\qquad$ ones/tens/hundreds subtract $\qquad$ ones/tens/ hundreds is equal to $\qquad$
- I can/cannot subtract $\qquad$ ones/tens/hundreds from $\qquad$ ones/tens/hundreds, so I do/do not need to make an exchange.


## National Curriculum links

- Add and subtract numbers with up to four digits using the formal written methods of columnar addition and subtraction where appropriate
- Solve addition and subtraction two-step problems in contexts, deciding which operations and methods to use and why


## Subtract two 4-digit numbers - more than one exchange

## Key learning

- Tommy uses base 10 to help him work out 4,052-2,415


Use Tommy's method to work out the subtractions.

- Mr Jones paid £8,562 for his car.

Mrs Smith paid $£ 6,729$ for her car.
How much more did Mr Jones pay for his car than Mrs Smith paid for hers?

- Aisha works out 3,206-2,148 using place value counters.


Use Aisha's method to work out the subtractions.


- A shop has 8,435 magazines.

It sells 367 in the morning and 579 in the afternoon.
How many magazines are left?

| 8,435 |  |  |
| :--- | :--- | :--- |
| 367 | 579 |  |

Explain how you found the answer.
Is there more than one way to solve this problem?

## Subtract two 4-digit numbers - more than one exchange

## Reasoning and problem solving

Tiny has worked out 3,035-1,074


Do you agree with Tiny?
Explain your answer.


Find the missing 4-digit number.


How did you find the answer?
Is there more than one way?

Work out
2,114-650 for the number of visitors on Sunday.
3,578
650 more people visited the museum on Saturday than on Sunday.

Altogether, how many people visited the museum over the two days?

What do you need to do first to solve the problem?
-

There were 2,114 visitors to a museum on Saturday.

## Notes and guidance

Having explored both mental and written methods of subtraction in this block, the purpose of this small step is to encourage children to make choices about which method is most appropriate for a given calculation. Children can often become reliant on formal written methods, so it is important to explicitly highlight where mental strategies or less formal jottings can be more efficient.

Children explore the concept of constant difference, where adding or subtracting the same amount to/from both numbers in a subtraction means that the difference remains the same, for example $2,832-1,999=2,833-2,000$ or $400-193=399-192$. This can help make potentially tricky subtractions with multiple exchanges much simpler, sometimes even becoming calculations that can be performed mentally. Number lines can support understanding of this concept.

## Things to look out for

- Children may be overly reliant on formal written methods and use them when alternative strategies are more appropriate.
- Children may not adjust both numbers in the subtraction.


## Key questions

- Which method do you find easiest? Why?
- Which method is most efficient?
- Can you work this out mentally?
- What does "difference" mean?
- What does the arrow represent? What do you notice about all the arrows?
- Why does adding/subtracting ___ to/from each number make the calculation easier?


## Possible sentence stems

- The jump to the next multiple of $\qquad$ is $\qquad$
- If I add/subtract $\qquad$ to/from both numbers, the difference will be the same.


## National Curriculum links

- Add and subtract numbers with up to four digits using the formal written methods of columnar addition and subtraction where appropriate


## Efficient subtraction

## Key learning

- Kim, Tom and Huan are working out 203-198



Whose method do you prefer? Why?
Which is the most efficient method?
Use your preferred method to complete the subtractions.

$$
9,807-9,792
$$

$$
809-15
$$

$$
3,876-1,400
$$

$$
4,204-2,417
$$

Did you use the same method each time?

- Complete each subtraction.

What do you notice?
What stays the same?
What changes?


- Eva is working out 357-199


Use Eva's method to work out the subtractions.

$$
\begin{array}{l|l}
3,487-999 & 4,407-1,399
\end{array}
$$

$7,643-5,098$

- Complete the subtractions.

| $300-176 \quad 4,000-3,180 \quad 6,001-3,065$ |
| :---: | :---: |

Compare methods with a partner.

## Efficient subtraction

## Reasoning and problem solving



Do you agree with Dexter?
Explain your reasons.
What other methods could
Dexter use?

Dora is working out 500-287


Dora needed to subtract 1 from both numbers.

213
e.g. $499-287=212$,
$212+1=213$
number lines

## Estimate answers

## Notes and guidance

In Year 3, children explored the idea of estimating without explicitly using the language of rounding. Now that children have covered rounding in Autumn Block 1, they are familiar with the language of "rounding to the nearest $\qquad$ ". In this small step, children estimate by rounding to the nearest ten, hundred and thousand. Number lines are a useful representation to support this understanding.

Discuss why estimates are important, particularly in real-life situations such as population statistics. They allow us to quickly and easily get an idea of what an answer should be near to or if an already calculated answer is appropriate. It is important to discuss whether an actual answer will be greater or less than an estimate. For example, $333+524$ may be estimated as $300+500$, and the precise answer will be greater than the estimate because both the numbers were rounded to the previous multiple.

## Things to look out for

- Children may find it difficult to decide which multiple to round to.
- Children may find it difficult to work out whether an estimate will be greater or less than the actual answer.


## Key questions

- What multiple of 10/100/1,000 comes before and after $\qquad$ ?
- Where would $\qquad$ be on this number line?
- Which multiple is $\qquad$ closer to?
- Which calculation is easier/quicker to perform? Why?
- Why do we use estimates?
- Is the estimate less than or greater than the actual answer? Why?


## Possible sentence stems

- $\qquad$ is closer to $\qquad$ than $\qquad$
- So ___ rounded to the nearest $\qquad$ is $\qquad$
- The estimate will be $\qquad$ than the actual answer because ...


## National Curriculum links

- Estimate and use inverse operations to check answers to a calculation


## Estimate answers

## Key learning

- Use the number lines to help you complete the sentences.


1,880 rounded to the nearest thousand is $\qquad$


3,341 rounded to the nearest thousand is $\qquad$
Use the rounded amounts to estimate 3,341-1,880
Use column subtraction to work out the actual answer.

- Write < or > to complete the statements.

$327+436 \bigcirc 327+400$

$8,000-3,838 \bigcirc 8,000-4,000$

$4,000-1,132 \bigcirc 400-1,100$

What do you notice?

- Annie and Tommy are estimating the answer to 3,219 + 5,624


Use Annie and Tommy's methods to estimate the answer.
Now work out the actual answer using column addition.
Whose estimate was more accurate? Why?

- Mrs Lee has $£ 5,000$ in her bank account.

A TV costs $£ 1,328$
A car costs $£ 3,889$
Estimate whether Mrs Lee can afford to buy both the television and the car.

Does your answer change if you round to a different amount?

## Estimate answers

## Reasoning and problem solving



The estimated answer to a calculation is 3,400

The numbers in the calculation were rounded to the nearest hundred for the estimate.

What could the original calculation be?

Ron and Sam

Sam's

Ron's
$\square$

Roll a 6-sided dice eight times.
Write each number in one of the boxes.
Now work out your addition.


Compete against a partner. Who can get an answer closest to 5,000?
multiple possible answers, e.g.
$2,343+1,089$
4,730-1,304

Compare answers as a class.

## Checking strategies

## Notes and guidance

In this small step, children explore the inverse relationship between addition and subtraction. From learning in earlier years, children know that addition and subtraction are inverse operations and they should also be aware that addition is commutative and subtraction is not.

Bar models and part-whole models are useful representations to help establish families of facts that can be found from one calculation. Children use inverse operations to check the accuracy of their calculations, rather than simply redoing the same calculation and potentially repeating the same error.

Estimations can be used alongside inverse operations as an alternative checking strategy.

## Things to look out for

- Children may subtract a part from a part rather than a part from the whole, for example writing $240-130$ as the inverse of $240+130$
- When asked to check an answer, children may just repeat the same calculation instead of using the inverse operation.


## Key questions

- What are the parts? What is the whole?
- Given one fact, what other facts can you write?
- What does "inverse" mean?
- What is the inverse of add/subtract $\qquad$ ?
- Is addition/subtraction commutative?


## Possible sentence stems

- The inverse of $\qquad$ is $\qquad$
- If $\qquad$ is a part and $\qquad$ is a part, then $\qquad$ is the whole.
- If $\qquad$ is the whole and $\qquad$ is a part, then $\qquad$ is the other part.
- To check I have added/subtracted $\qquad$ correctly, I need to $\qquad$


## National Curriculum links

- Estimate and use inverse operations to check answers to a calculation


## Checking strategies

## Key learning

- Complete the part-whole models and number sentences.

$1,500+800=$ $\qquad$ $2,300-1,500=$ $\qquad$ $2,300-800=$ $\qquad$

How could you check your answers?

- Complete the bar model for $3,582-2,236=1,346$


Use the bar model to write the fact family.

- Which subtractions can be used to check the addition $1,574+3,432=5,006 ?$
$5,006-3,432 \quad 5,006-1,574 \quad 3,432-1,574 \quad 1,574-5,006$
- Which additions can be used to check the subtraction $3,265-823=2,442$ ?

- Use an inverse operation to check each calculation.

How many different inverse calculations can you do for each?

|  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Th | $\mathbf{H}$ | $\mathbf{T}$ | $\mathbf{O}$ |  |
|  |  | 4 | 5 | 1 | 9 |  |
|  | + |  | 7 | 2 | 3 |  |
|  | 5 | 2 | 4 | 2 |  |  |
|  |  | 1 |  | 1 |  |  |
|  |  |  |  |  |  |  |


|  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Th | $\mathbf{H}$ | $\mathbf{T}$ | $\mathbf{O}$ |  |
|  |  | 3 | ${ }^{4}$ \& | 1 | 6 | 4 |
|  | - | 1 | 4 | 8 | 4 |  |
|  | 2 | 0 | 8 | 0 |  |  |
|  |  |  |  |  |  |  |

- Dani has answered a problem.

Mr Rose has $£ 2,358$ in his bank account.
He spends $£ 1,209$ on a family holiday.
How much does he have left?

Estimate to check Dani's answer.
Now use an inverse calculation to check if Dani's answer is correct.

## Checking strategies

## Reasoning and problem solving



Show by estimating that Tiny has made a mistake.
What mistake has Tiny made?
Find the correct answer.
Complete an inverse operation to check your answer.

Tiny is completing some statements.

Check Tiny's answers.
Do you need to work out the answers or can an estimate help you decide whether Tiny is correct?

$$
\begin{aligned}
& 55+28=70-13 \\
& 55-28=13+40 \\
& 28+\boxed{12}>55-13 \\
& 28+13<55-96
\end{aligned}
$$

Find the correct answers.
Is there more than one possible answer for any of the statements?

Compare strategies as a class.

## 96

14
any number greater than 14
any number between 0 and 13

